

# Causal Data Science:

A general framework for data fusion  
and causal inference

Elias Bareinboim

Columbia University

Twitter: [@eliasbareinboim](https://twitter.com/eliasbareinboim)

MIT Graphical Models Workshop  
Boston, August, 2019

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A general framework for data fusion  
and causal inference

(On the Causal Foundations of Data Science)

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# The aspirations & challenges of modern Data Science (circa 2019)

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Hal Varian, chief economist at Google and UC Berkeley  
Professor of Information Sciences, Business, and Economics.

# The aspirations & challenges of modern Data Science (circa 2019)

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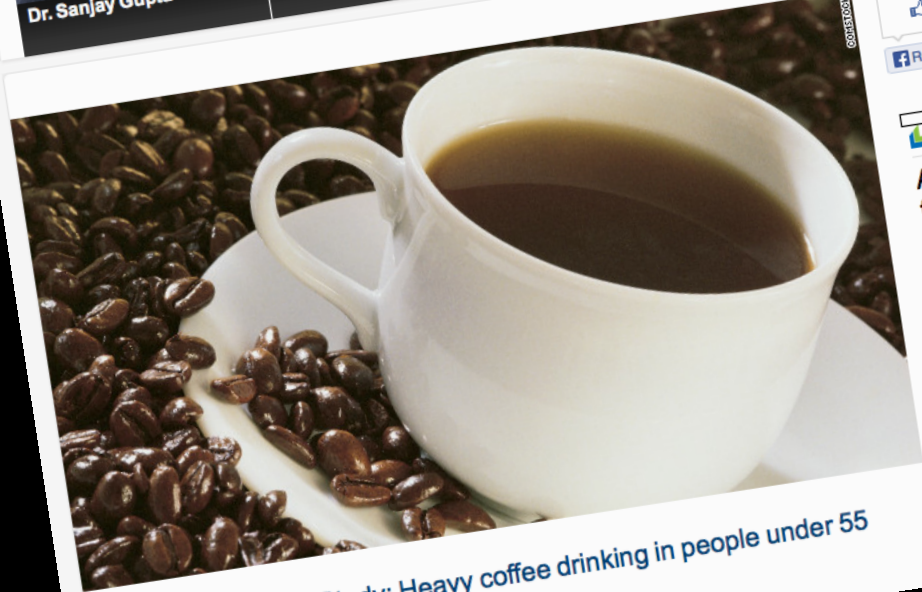
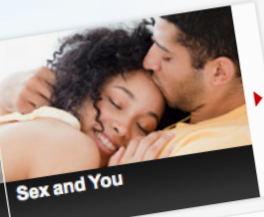
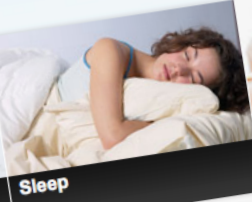
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# The aspirations & challenges of modern Data Science (circa 2019)

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Hal Varian, chief economist at Google and UC Berkeley  
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- *“Big data is not about the data!”*  
Gary King, Political Scientist, University Professor, Harvard University.
- *“Data Science is only as much of a science as it facilitates the interpretation of data - a two body problem, connecting data to reality”.*  
Judea Pearl, Professor of Computer Science & Statistics, UCLA.

# CURRENT STATE OF AFFAIRS (REPORT FROM THE TRENCHES)



August 15th, 2013  
08:00 PM ET

## Study: Heavy coffee drinking in people under 55 linked to early death

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Are you aware of any of the following?  
 UnitedHealthcare  Humana  
 Aetna  Blue Cross

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Only 5 questions? Easy.

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## the chart



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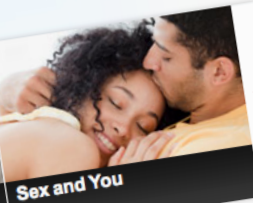
Children's Health



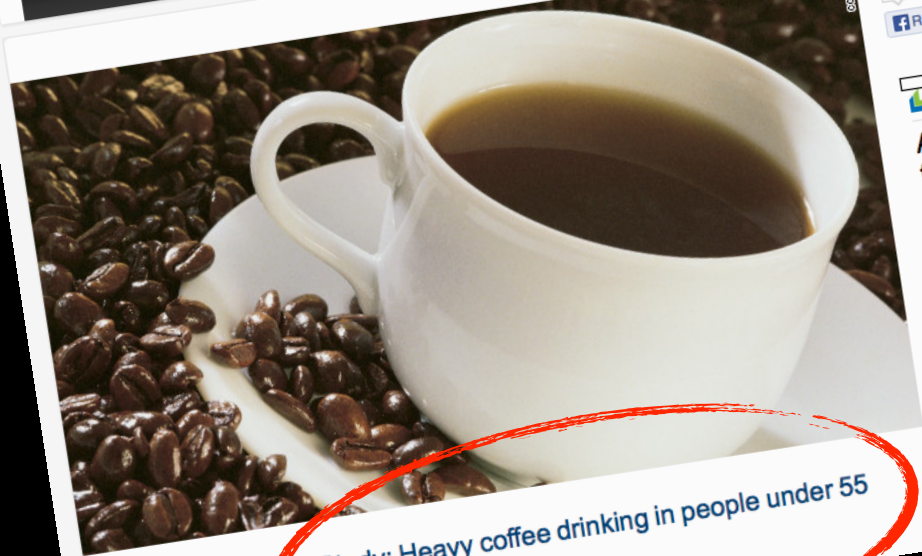
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### Study: Heavy coffee drinking in people under 55 linked to early death

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17 June 2008, Vol 148, No. 12 >

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Articles 17 June 2008 PDF

## The Relationship of Coffee Consumption with Mortality

Esther Lopez-Garcia, PhD; Rob M. van Dam, PhD; Tricia Y. Li, MD; Fernando Rodriguez-Artalejo, MD, PhD; and Frank B. Hu, MD, PhD

[+] Article and Author Information

Ann Intern Med. 2008;148(12):904-914. doi:10.7326/0003-4819-148-12-200806170-00003

Text Size: **A** A A

- Article
- Figures
- Tables
- References
- Audio/Video
- Summary for Patients
- Comments (2)

### Abstract

[Abstract](#) | [Context](#) | [Contribution](#) | [Caution](#) | [Methods](#) | [Results](#) | [Discussion](#) | [References](#)

**Background:** Coffee consumption has been linked to various beneficial and detrimental health effects, but data on its relation with mortality are sparse.

**Study:** Heavy ~ linked to early death

August 15th, 2013  
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By MICHELLE CASTILLO CBS NEWS February 15, 2013, 3: 36 PM

# Alcohol causes 20,000 cancer deaths in the U.S. annually



Dr. Sa



August 15  
08:00 PM E

In Texas it is illegal to take more than three sips of beer at a time while standing. / AP / FILE

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the Clinic Journal Club CME



## Mortality

jo, MD, PhD; and Frank

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More +

cial and detrimental health effects,



# One Drink Of Red Wine Or Alcohol Is Relaxing To Circulation, But Two Drinks Are Stressful

Feb. 13, 2008 — One drink of either red wine or alcohol slightly benefits the heart and blood vessels, but the positive effects on specific biological markers disappear with two drinks, say researchers at the Peter Munk Cardiac Centre of the Toronto General Hospital.

## Related Topics

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- ▶ Heart Disease
- ▶ Hypertension

### Mind & Brain

### Articles

- ▶ Mediterranean diet
- ▶ Drunkenness
- ▶ Coronary heart disease



# One Drink Of Red Wine Or Alcohol Is Relaxing To Circulation, But Two Drinks Are Stressful

Feb. 13, 2008 — One drink of either red wine or alcohol slightly but the positive disappear with Peter Munk Ca Hospital.

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## Why Do Heavy Drinkers Outlive Nondrinkers?

One of the most contentious issues in the vast literature about alcohol consumption has been the consistent finding that those who don't drink tend to die sooner than those who do.

By John Cloud Monday, Aug. 30, 2010

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Correction Appended: Aug. 31, 2010

One of the most contentious issues in the vast literature about alcohol consumption has been the consistent finding that those who don't drink tend to die sooner than those who do. The standard Alcoholics Anonymous explanation for this finding is that many of those who show up as abstainers in such research are actually former hard-core drunks who had already incurred health problems associated with drinking.



Jodi Cobb / National Geographic Creative / Getty Images

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# Science News

## One Drink Of Red Wine Or Drinks Are Stressful

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alcohol slightly  
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One of the most conter  
consistent finding'

By John Cloud

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#### Correction Appen

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with drinking.

August 15  
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# The NEW ENGLAND JOURNAL of MEDICINE

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ORIGINAL ARTICLE

## Association of Nut Consumption with Total and Cause-Specific Mortality

Ying Bao, M.D., Sc.D., Jiali Han, Ph.D., Frank B. Hu, M.D., Ph.D., Edward L. Giovannucci, M.D., Sc.D., Meir J. Stampfer, M.D., Dr.P.H., Walter C. Willett, M.D., Dr.P.H., and Charles S. Fuchs, M.D., M.P.H.  
N Engl J Med 2013; 369:2001-2011 | November 21, 2013 | DOI: 10.1056/NEJMoa1307352

Abstract Article References

### BACKGROUND

Increased nut consumption has been associated with a reduced risk of major chronic diseases, including cardiovascular disease and type 2 diabetes mellitus. However, the association between nut consumption and mortality remains unclear.

### METHODS

We examined the association between nut consumption and

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WHAT'S GOING ON HERE?

WHAT'S GOING ON HERE?





WHAT'S GOING ON HERE?



Eli's thesis: Mismatch between the type of data collected & desired claim.

# TASKS

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- Develop machinery (language, conditions, and algorithms) for performing two tasks:



# TASKS

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1. **Learning** about population-level interventions by cohesively combining multiple heterogeneous datasets

(NeurIPS'14, PNAS'16, AAAI'17, UAI'18).

Causal inference and the data-fusion problem

Elias Bareinboim and Judea Pearl

PNAS July 5, 2016 113 (27) 7345-7352; published ahead of print July 5, 2016 https://doi.org/10.1073/pnas.1510507113

Edited by Richard M. Shiffrin, Indiana University, Bloomington, IN, and approved March 15, 2016 (received for review June 29, 2015)



- Article
Email
Citation
Requirements

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1. Learning about p interventions by conesively combining multiple heterogenous datasets

(NeurIPS'14, PNAS'16, AAAI'17, UAI'18).

# TASKS

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# TASKS

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1. **Learning** about population-level interventions by cohesively combining multiple heterogeneous datasets

(NeurIPS'14, PNAS'16, AAAI'17, UAI'18).

2. **Deciding** individual-level treatments by leveraging population-level knowledge

(NeurIPS'15, ICML'17, NeurIPS'18, AAAI'19).

DATA, DATA, DATA...

Challenge: “All data is not created equal”

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# DATA, DATA, DATA...

## Challenge: “All data is not created equal”

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- Key observation. There’s a lot of data out there, but this data is almost invariably collected...
  - under different **experimental conditions**,

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  - many variables are **not measured**.
- In words, the collected data is messy, and rarely perfectly matches the inferential target.
- Positive: All these dimensions are now formalized.
- And there are conditions and algorithms to decide what is “entailed” from a certain data collection.

# HETEROGENEOUS DATASETS

---

Target

$$Q = P^*(y | \text{do}(x))$$

# HETEROGENEOUS DATASETS

---

Target

$$Q = P^*(y | \text{do}(x))$$

vs  $P^*(y | x)$

# HETEROGENEOUS DATASETS

---

Target

$$Q = P^*(y | \text{do}(x))$$



# HETEROGENEOUS DATASETS

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Target  
 $Q = P^*(y | do(x))$

Dataset 1

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Dataset 2

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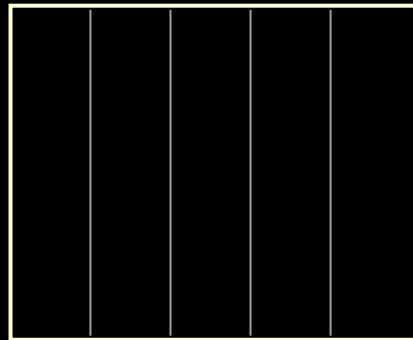
Dataset n

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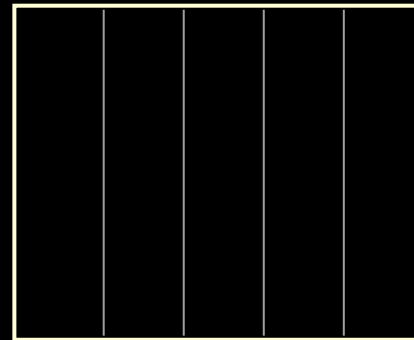
# HETEROGENEOUS DATASETS

Target  
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Dataset 1

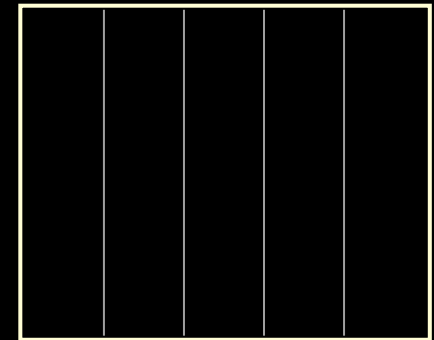


Dataset 2



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Dataset n

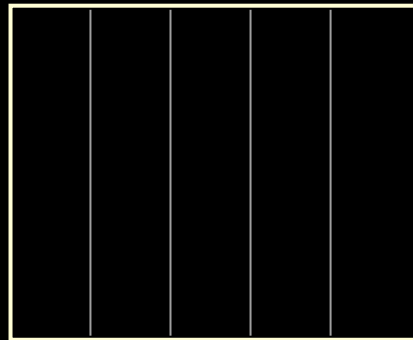


Population	Los Angeles	New York	Texas
Obs. / Exp.	Experimental	Observational	Experimental
Treat. Assign.	Randomized $Z_1$	-	Randomized $Z_2$
Sampling	Selection on Age	Selection on SES	-
Measured	$X_1, Z_1, W, M, Y_1$	$X_1, X_2, Z_1, N, Y_2$	$X_2, Z_1, W, L, M, Y_1$

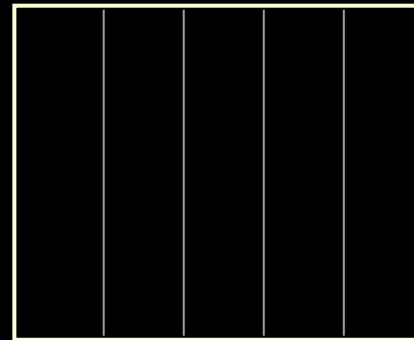
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Target  
 $Q = P^*(y | do(x))$

Dataset 1



Dataset 2



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Dataset n



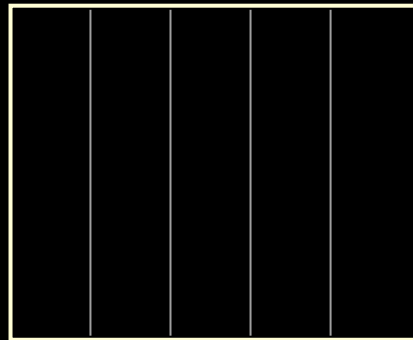
$d_1$

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Treat. Assign.	Randomized $Z_1$	-	Randomized $Z_2$
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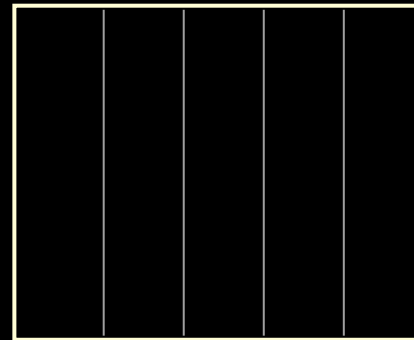
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Dataset 1

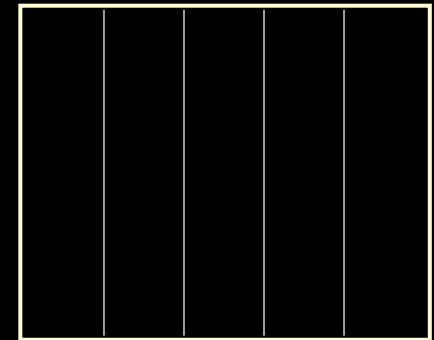


Dataset 2



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Dataset n



$d_1$

Population	Los Angeles	New York	Texas
Obs. / Exp.	Experimental	Observational	Experimental
Treat. Assign.	Randomized $Z_1$	-	Randomized $Z_2$
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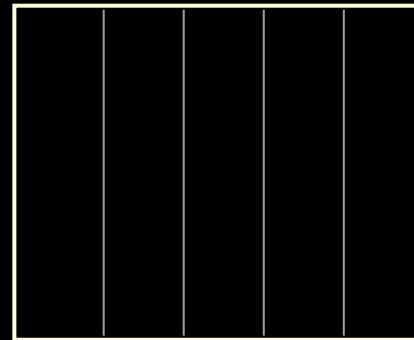
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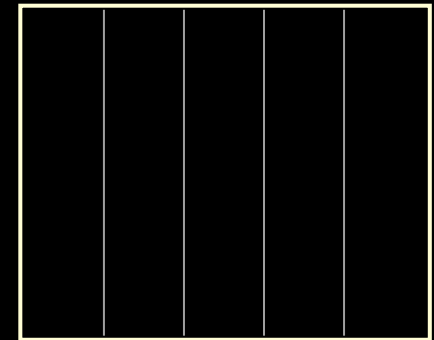


Dataset 2



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Dataset n

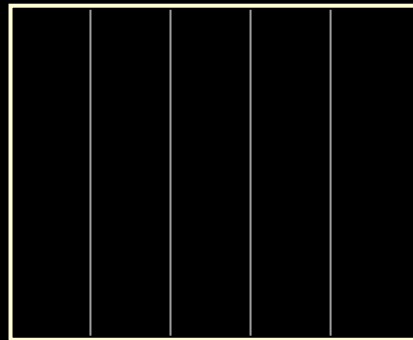


d <sub>1</sub>	Population	Los Angeles	New York	Texas
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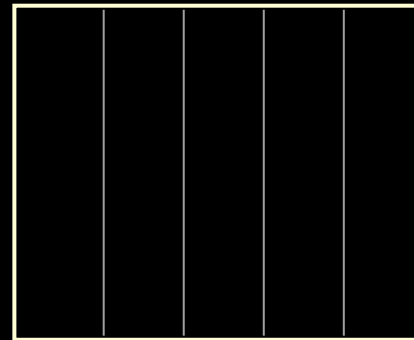
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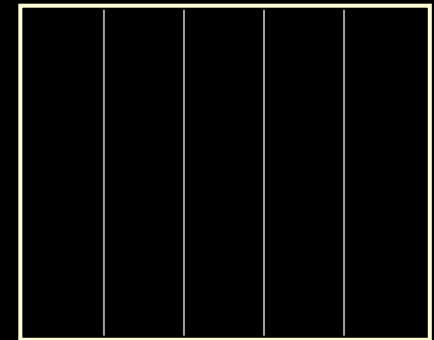


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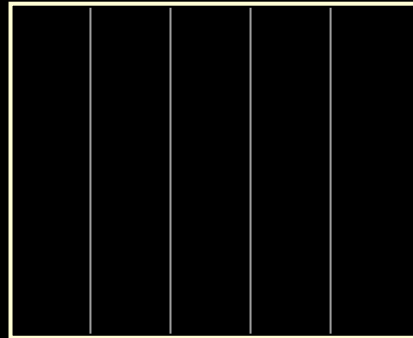


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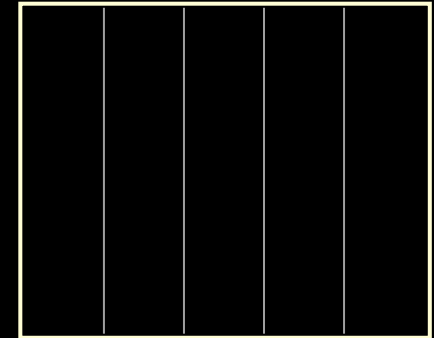


Dataset 2



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Dataset n

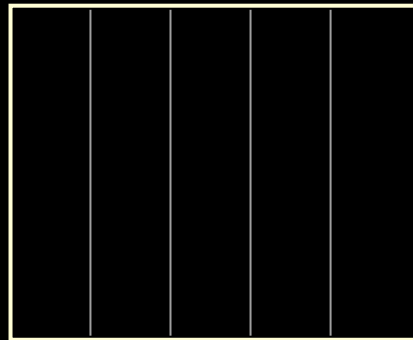


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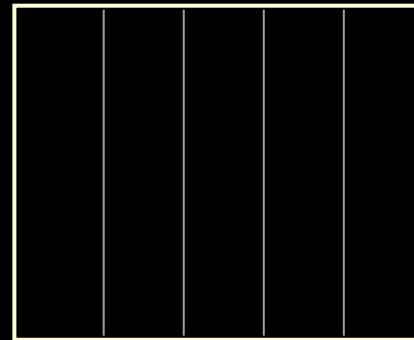
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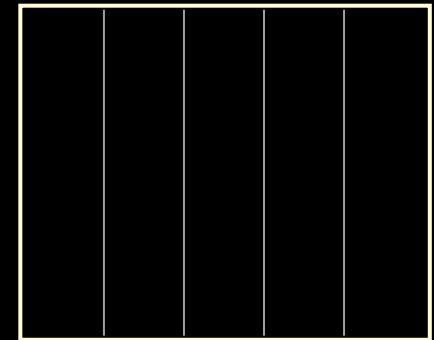


Dataset 2



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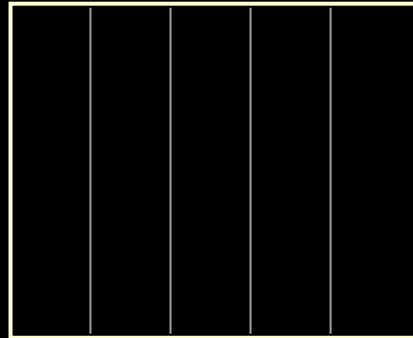
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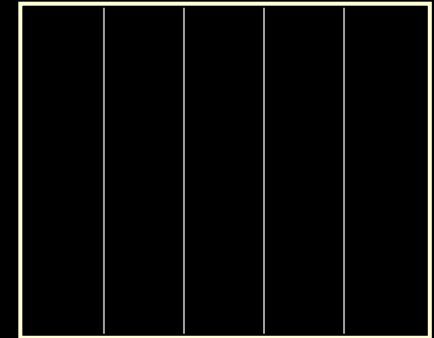


Dataset 2



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Dataset n



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	Treat. Assign.	Randomized Z <sub>1</sub>	-	Randomized Z <sub>2</sub>
d <sub>3</sub>	Sampling	Selection on Age	Selection on SES	-
d <sub>4</sub>	Measured	X <sub>1</sub> , Z <sub>1</sub> , W, M, Y <sub>1</sub>	X <sub>1</sub> , X <sub>2</sub> , Z <sub>1</sub> , N, Y <sub>2</sub>	X <sub>2</sub> , Z <sub>1</sub> , W, L, M, Y <sub>1</sub>

# HETEROGENEOUS DATASETS

**Target**  
 $Q = P^*(y | do(x))$

Dataset 1

--	--	--	--	--

Dataset 2

--	--	--	--	--

...

Dataset n

--	--	--	--	--

d <sub>1</sub>	<b>Population</b>	Los Angeles	New York	Texas
d <sub>2</sub>	<b>Obs. / Exp.</b>	Experimental	Observational	Experimental
	<b>Treat. Assign.</b>	Randomized Z <sub>1</sub>	-	Randomized Z <sub>2</sub>
d <sub>3</sub>	<b>Sampling</b>	Selection on Age	Selection on SES	-
d <sub>4</sub>	<b>Measured</b>	X <sub>1</sub> , Z <sub>1</sub> , W, M, Y <sub>1</sub>	X <sub>1</sub> , X <sub>2</sub> , Z <sub>1</sub> , N, Y <sub>2</sub>	X <sub>2</sub> , Z <sub>1</sub> , W, L, M, Y <sub>1</sub>

# CAUSAL DATA SCIENCE - DIMENSIONS & TASKS

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Some common inferences in scientific circles, AI, and machine learning involving some standard assumptions:

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Tasks

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a. Statistics – Descriptive

**Samples**(Obs) → **Distrib**(Obs)

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c. *Causal Inference from Observational Studies*

$\text{Distrib}(\text{Obs}) \rightarrow \text{Distrib}(\text{do}(X))$

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"Causal Inference" from ~1974-2011 was mainly concerned with **confounding bias**, and has been "solved" by Rubin, Robins, Dawid, Pearl.



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# CAUSAL DATA SCIENCE - DIMENSIONS & TASKS

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Also, this is “old stuff”, where does causal data science come into play?

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(population, obs./exp., sampling, measure.)

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Do these dimensions exhaust all possible data collection modes?

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Tasks

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$(\text{Bonobos}, d_2, d_3, d_4) \rightarrow (\text{Humans}, d_2, d_3, d_4)$

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EII: Special cases of these dimensions have been addressed in the literature, mostly in isolation, and under very special parametric conditions.

Tasks

In practice, they appear together in what I like to call **causal data science**,

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TRANSPORTABILITY:  
EXTRAPOLATION & ROBUSTNESS  
OF CAUSAL CLAIMS



# TRANSPORTABILITY - PROBLEM STATEMENT

---

Question:

Is it possible to **compute the effect of X on Y in a target environment  $\Pi^*$**  (where no experiments are feasible), using experimental findings from a **different environment  $\Pi$** ?

Answer: Sometimes **yes**.

# TRANSPORTABILITY - PROBLEM STATEMENT

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(or, external validity, robustness, generalizability)

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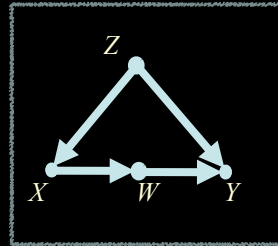
Answer: Sometimes **yes**.

Our goal is to formally characterize **when** and **how**.

# MOVING FROM THE “LAB” TO THE “REAL WORLD”...

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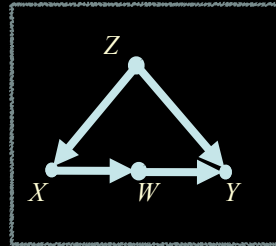
Lab



# MOVING FROM THE “LAB” TO THE “REAL WORLD”...

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Lab

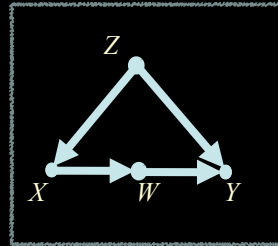


\* The lab stands for any environment, population, domain, setting.

# MOVING FROM THE “LAB” TO THE “REAL WORLD”...

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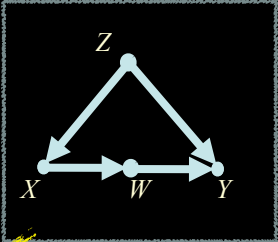
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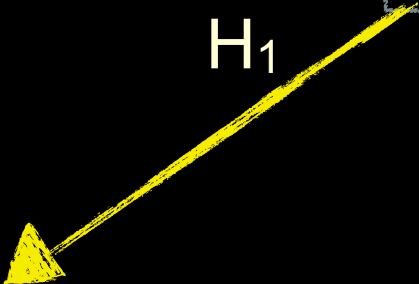
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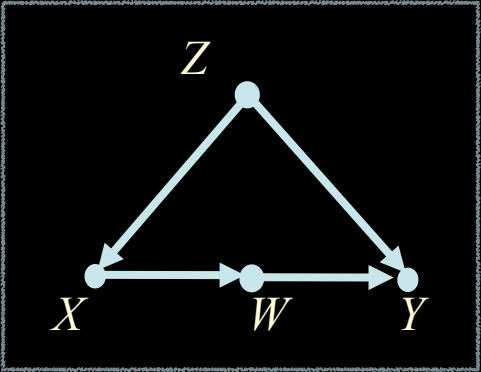
Lab



$H_1$



Real world

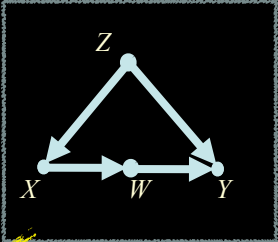


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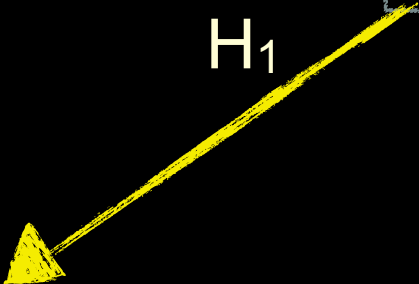
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$f_z = f^*_z$   
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 $f_w = f^*_w$   
 $f_y = f^*_y$

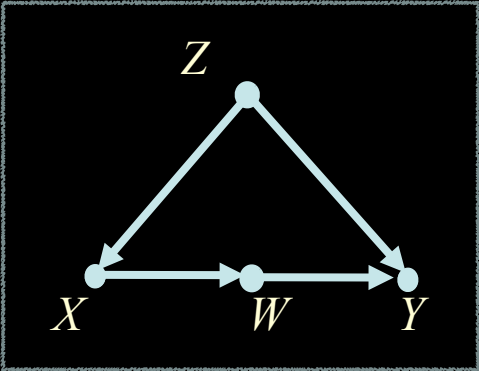
Lab



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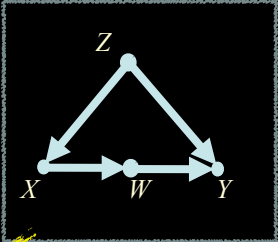


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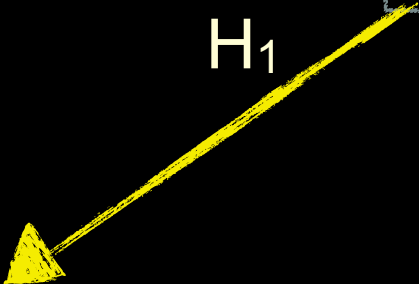
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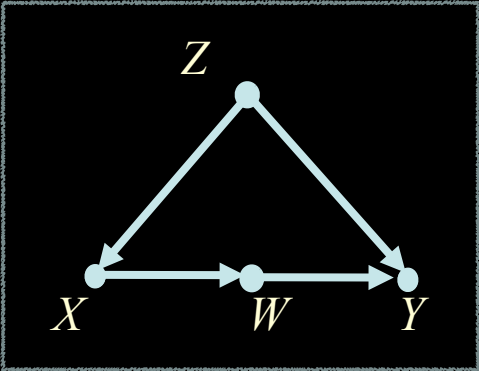
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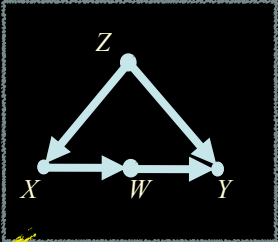


Everything is assumed to be the same, trivially transportable!

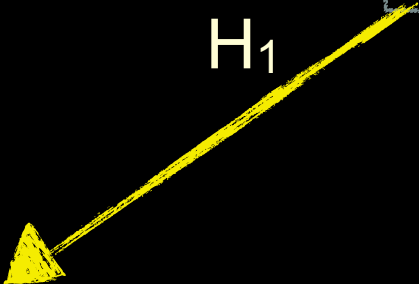
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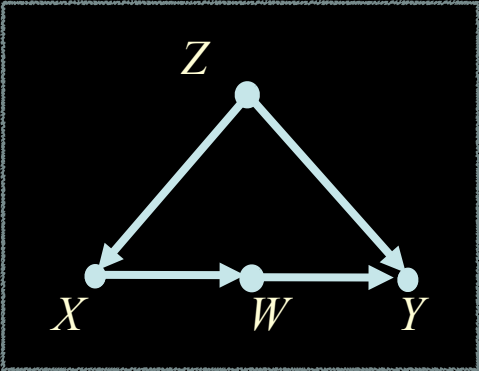
Lab



$H_1$

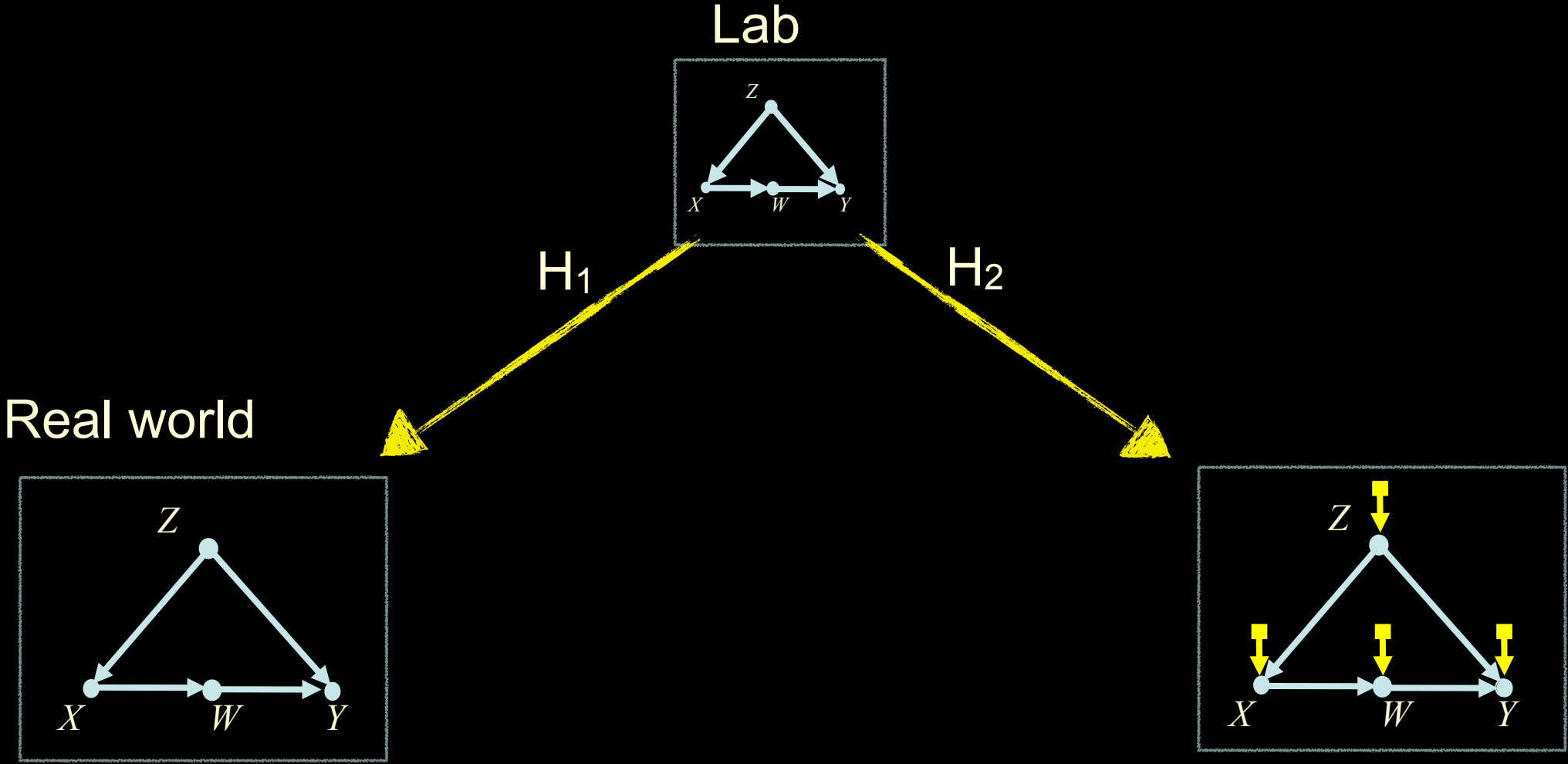


Real world



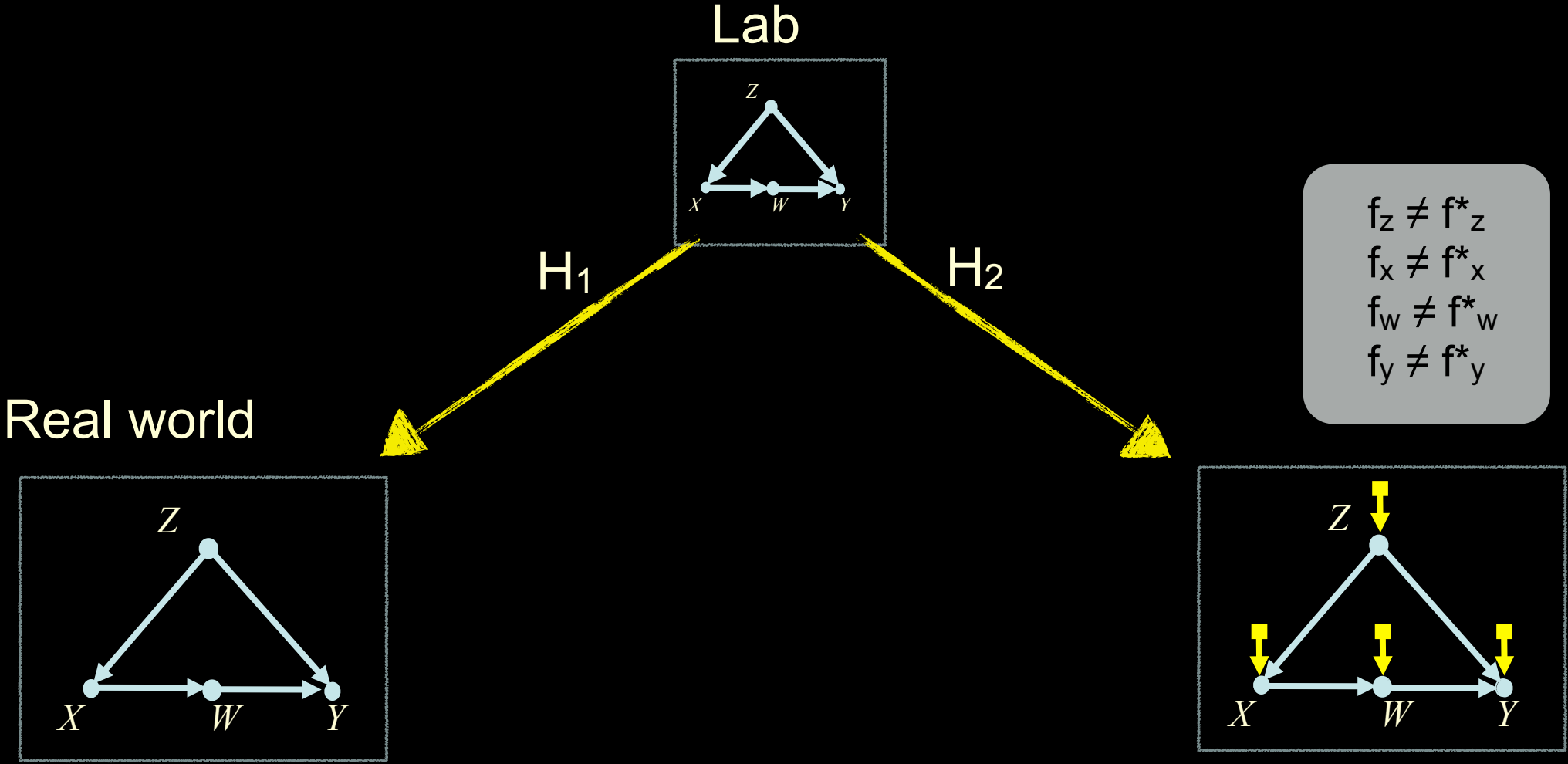
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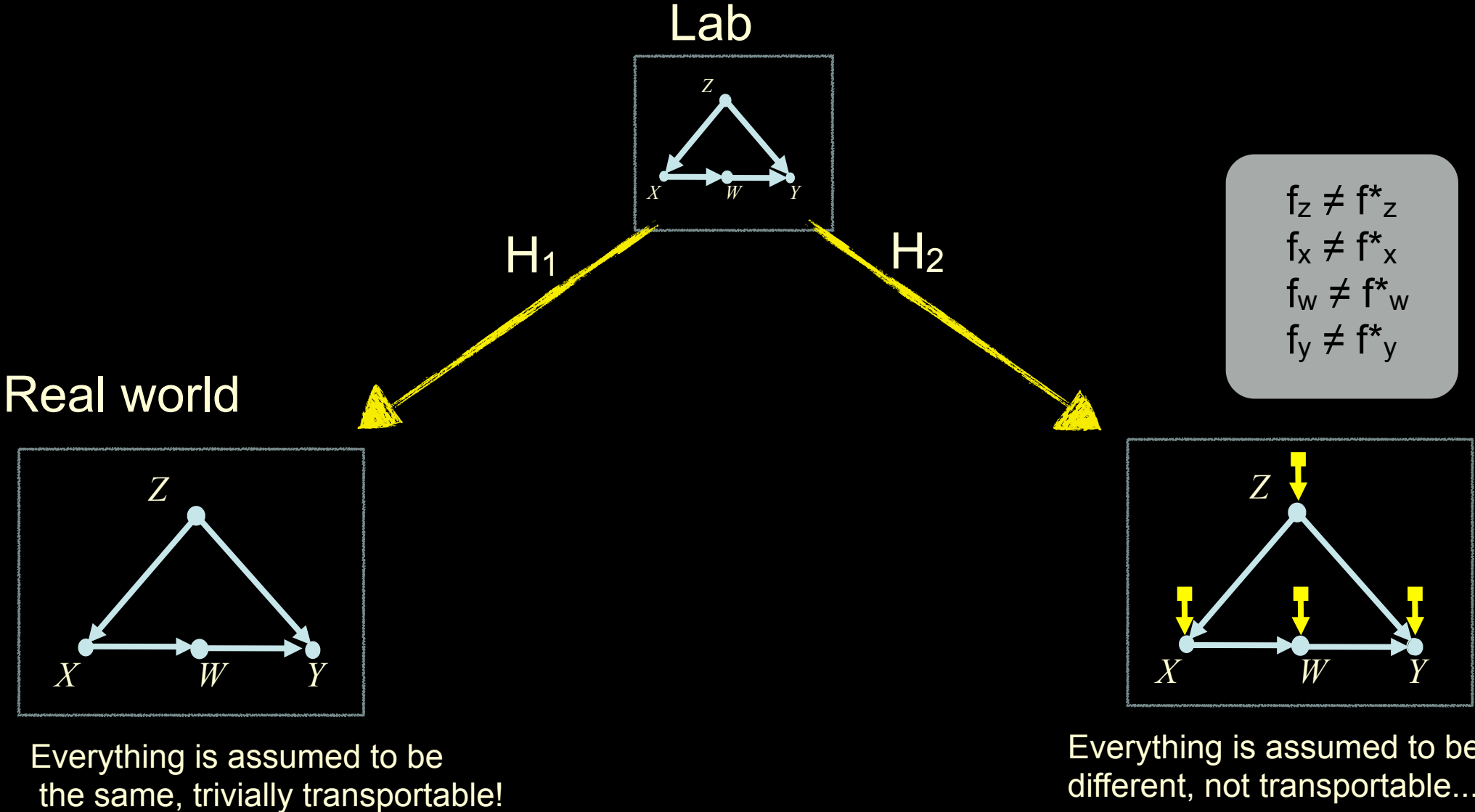
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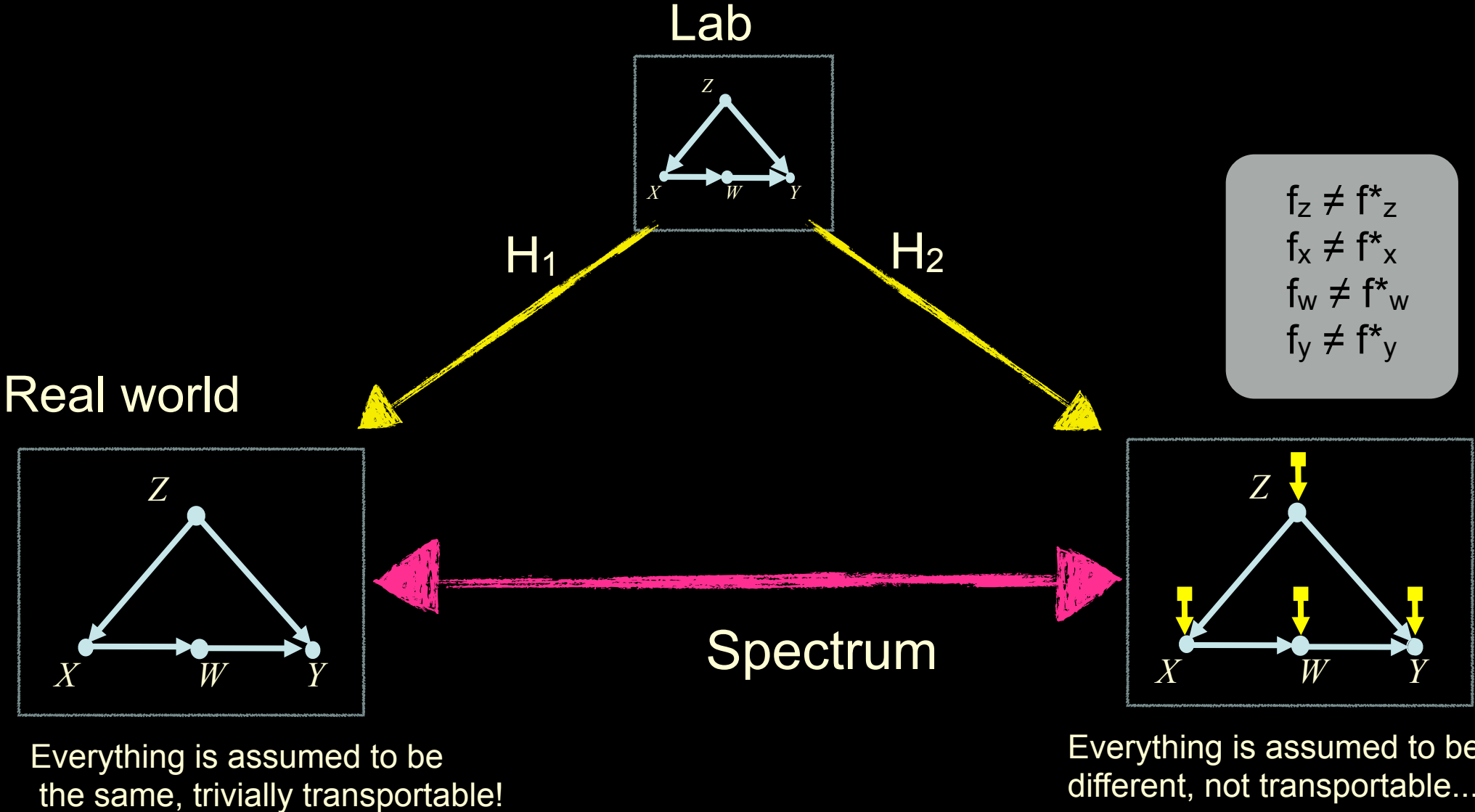


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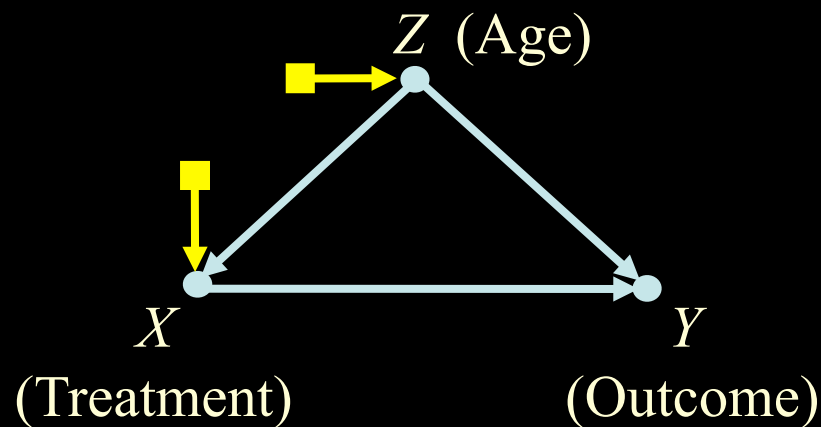
# MOVING FROM THE “LAB” TO THE “REAL WORLD”...



# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

---



$\Pi \rightarrow \Pi^*$   
LA NYC

# MOTIVATION

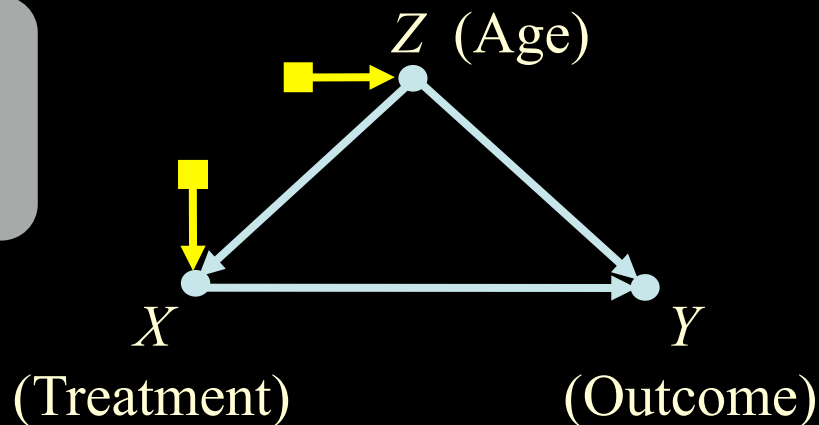
WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

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$$f_z \neq f_z^*$$

$$f_x \neq f_x^*$$

$$f_y = f_y^*$$



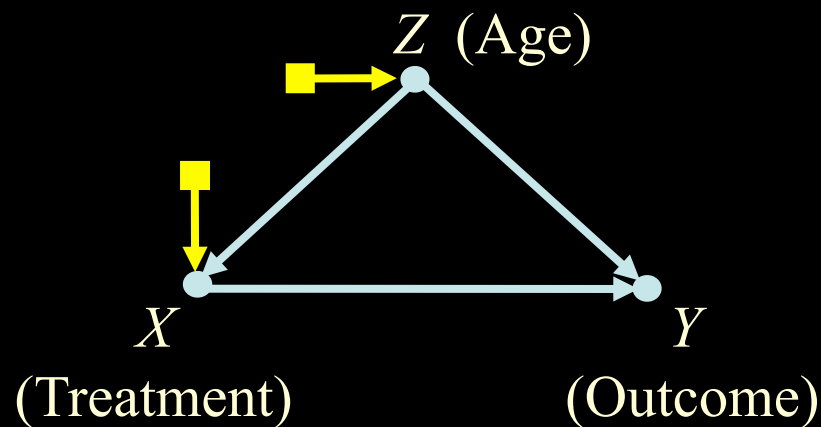
$\Pi \rightarrow \Pi^*$   
LA NYC



# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

---

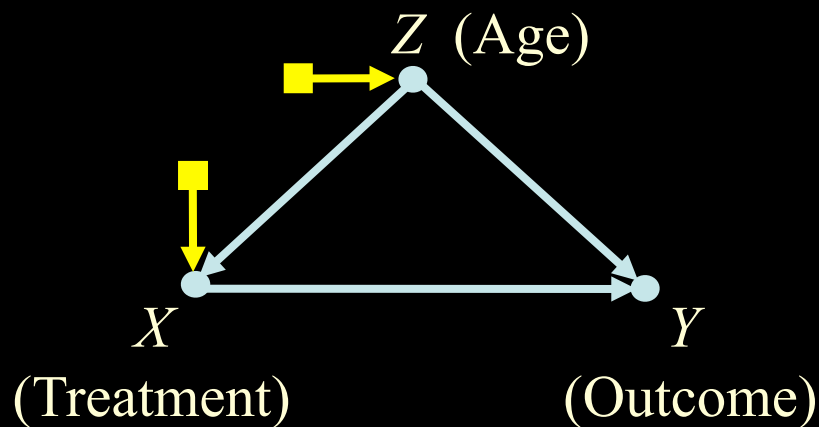


$\Pi \rightarrow \Pi^*$   
LA NYC

# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

Input

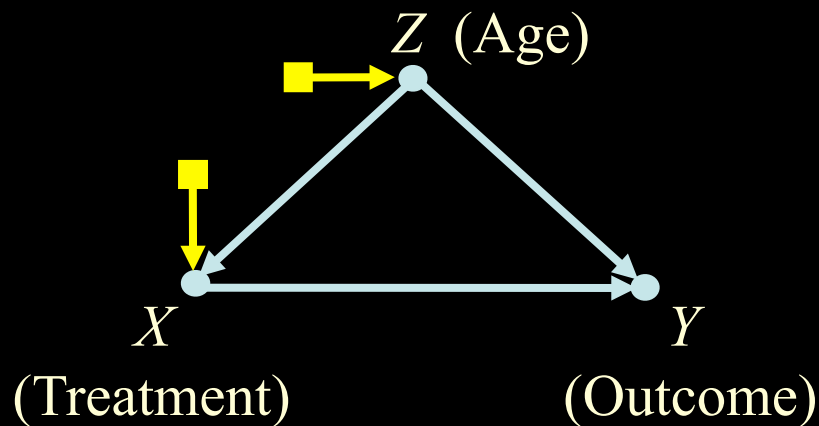


$\Pi \rightarrow \Pi^*$   
LA NYC

# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

Input



$\Pi \rightarrow \Pi^*$   
LA NYC

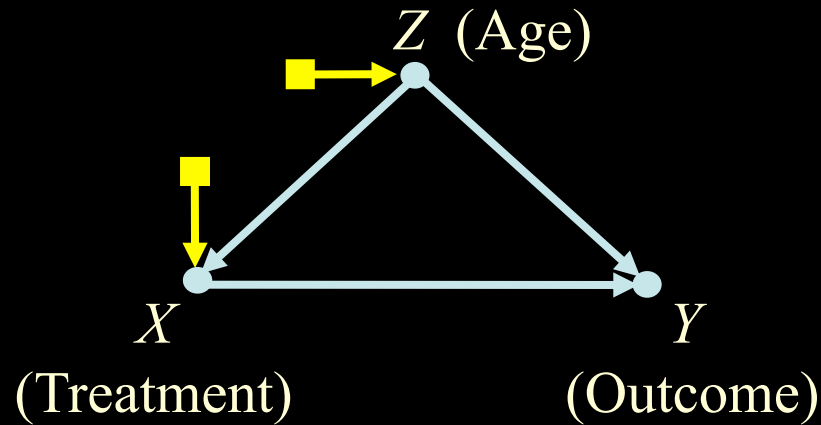
Experimental study in LA

Measured:  $P(x, y, z)$   
 $P(y \mid do(x), z)$

# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

Input



$\Pi \rightarrow \Pi^*$   
LA NYC

Experimental study in LA

Measured:  $P(x, y, z)$   
 $P(y \mid do(x), z)$

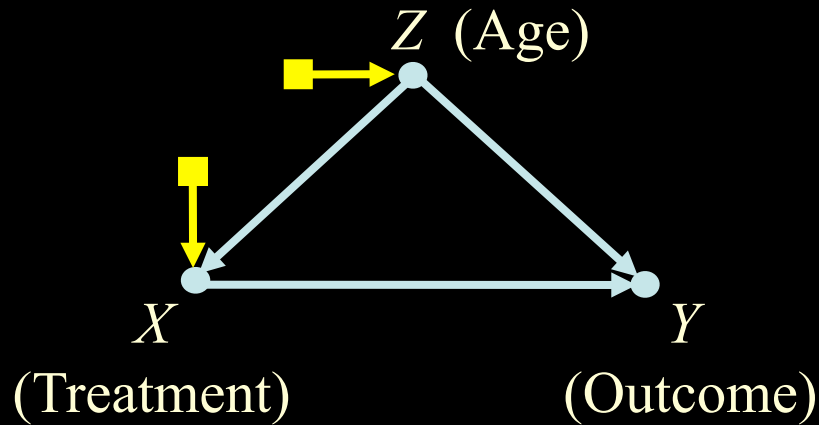
Observational study in NYC

Measured:  $P^*(x, y, z)$   
[  $P^*(z) \neq P(z)$  ]

# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

Input



$\Pi \rightarrow \Pi^*$   
LA NYC

Experimental study in LA

Measured:  $P(x, y, z)$   
 $P(y | do(x), z)$

Observational study in NYC

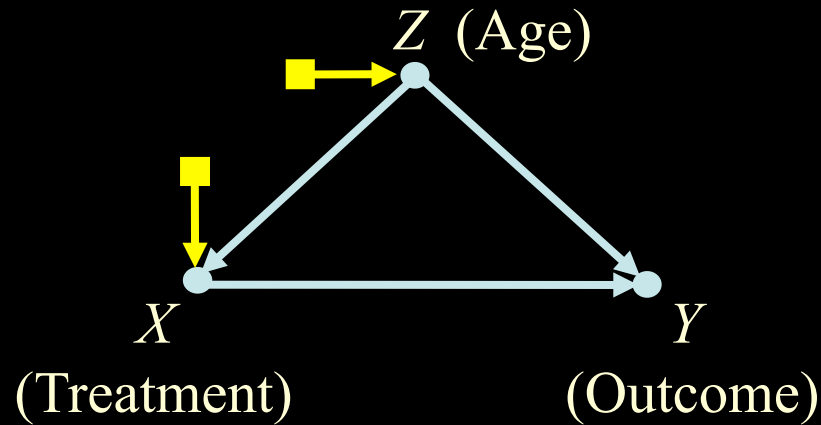
Measured:  $P^*(x, y, z)$   
[  $P^*(z) \neq P(z)$  ]

Needed:  $Q = P^*(y | do(x)) = ?$

# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

Input



$\Pi \rightarrow \Pi^*$   
LA NYC

Experimental study in LA

Measured:  $P(x, y, z)$   
 $P(y | do(x), z)$

Observational study in NYC

Measured:  $P^*(x, y, z)$   
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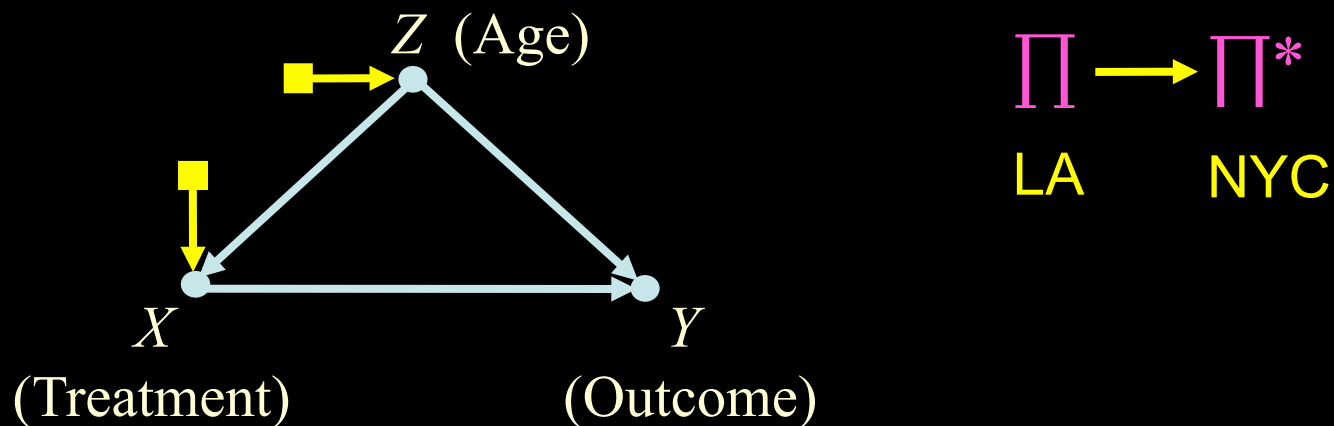
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Needed:  $Q = P^*(y | do(x)) = ?$

# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

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Experimental study in LA

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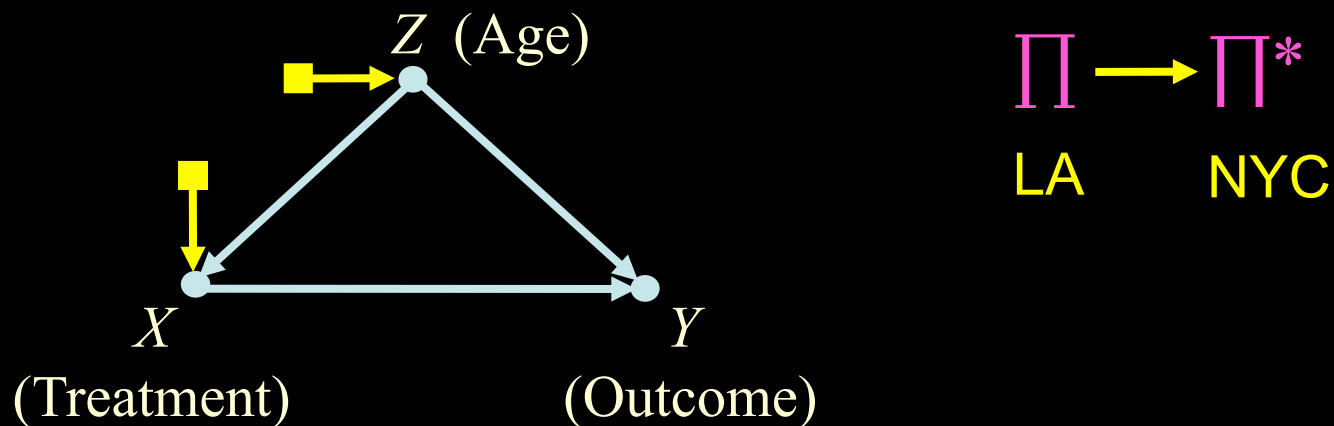
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# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

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Experimental study in LA

Measured:  $P(x, y, z)$   
 $P(y \mid do(x), z)$

Observational study in NYC

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[  $P^*(z) \neq P(z)$  ]

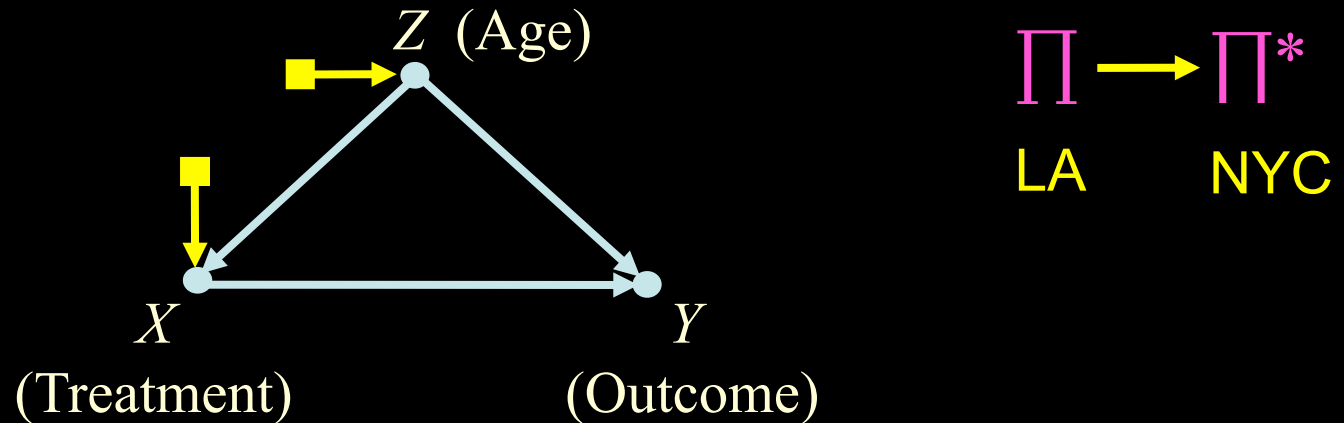
Needed:  $Q = P^*(y \mid do(x)) = \sum_z P(y \mid do(x), z) P^*(z)$



# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

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Experimental study in LA

Measured:  $P(x, y, z)$   
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Observational study in NYC

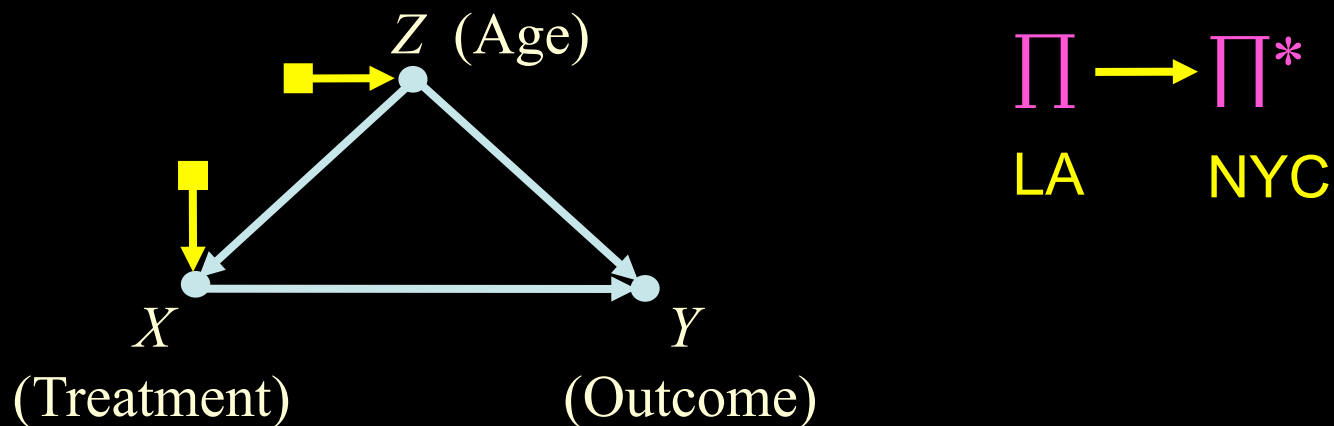
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# MOTIVATION

WHAT CAN EXPERIMENTS IN LA TELL US ABOUT NYC?

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Experimental study in LA

Measured:  $P(x, y, z)$   
 $P(y \mid do(x), z)$

Observational study in NYC

Measured:  $P^*(x, y, z)$   
[  $P^*(z) \neq P(z)$  ]

Needed:  $Q = P^*(y \mid do(x)) = \sum_z P(y \mid do(x), z) P^*(z)$

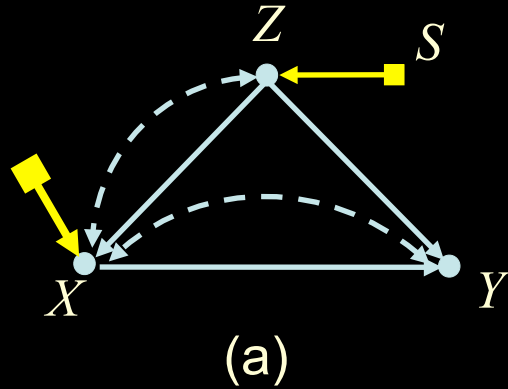
Transport Formula (recalibration):  $Q = F(P, P_{do}, P^*)$

# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS

---

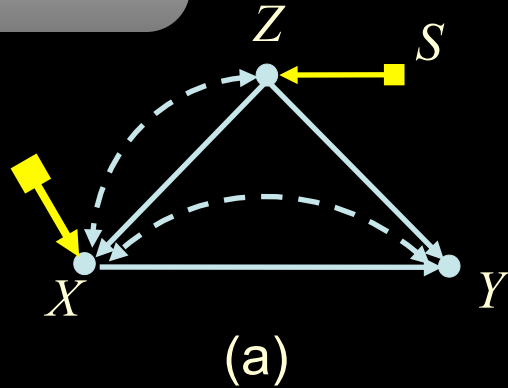
# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS

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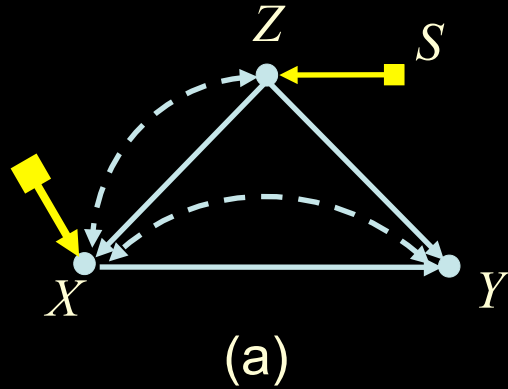
# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS

$$\begin{aligned} z &\leftarrow f_z(u_z, u_{xz}) \\ x &\leftarrow f_x(x, u_x, u_{xz}, u_{xy}) \\ y &\leftarrow f_y(x, z, u_y, u_{xy}) \end{aligned}$$



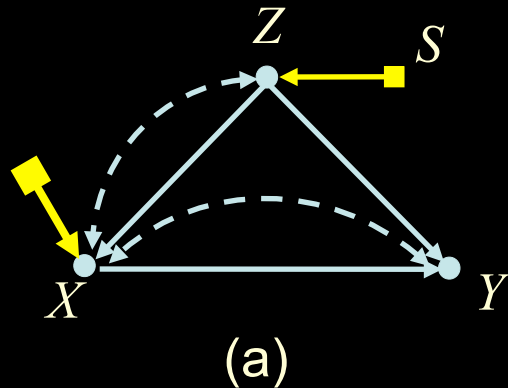
# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS

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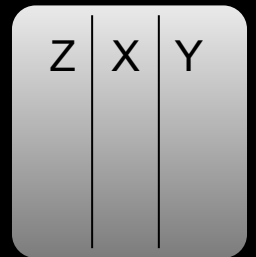


# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS

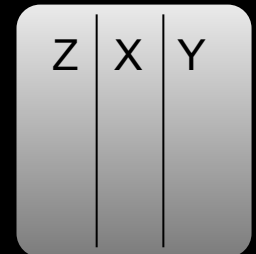
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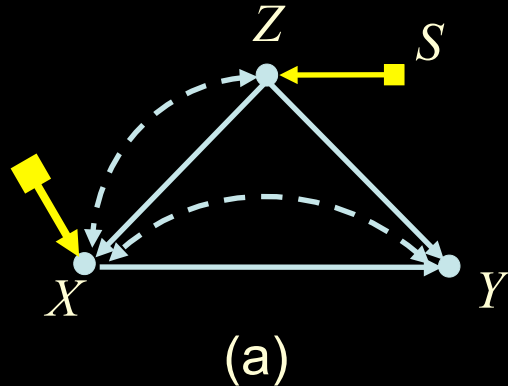
LA:  $P(y \mid \text{do}(x), z)$



NYC:  $P^*(x, y, z)$



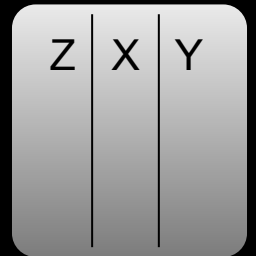
# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS



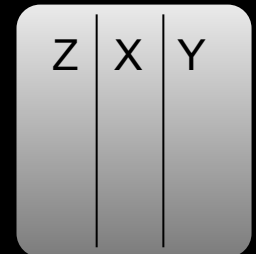
a)  $Z$  represents age

$$P^*(y | do(x)) = \sum_z P(y | do(x), z) P^*(z)$$

LA:  $P(y | do(x), z)$

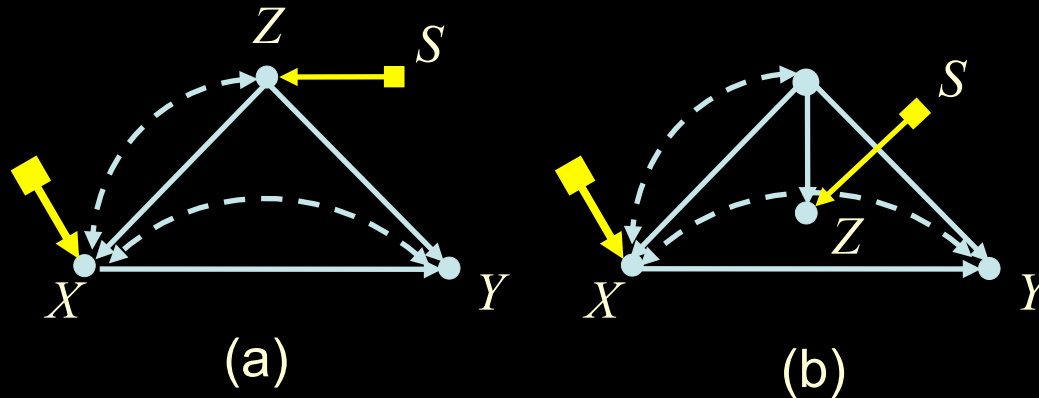


NYC:  $P^*(x, y, z)$





# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS



a)  $Z$  represents age

$$P^*(y | do(x)) = \sum_z P(y | do(x), z) P^*(z)$$

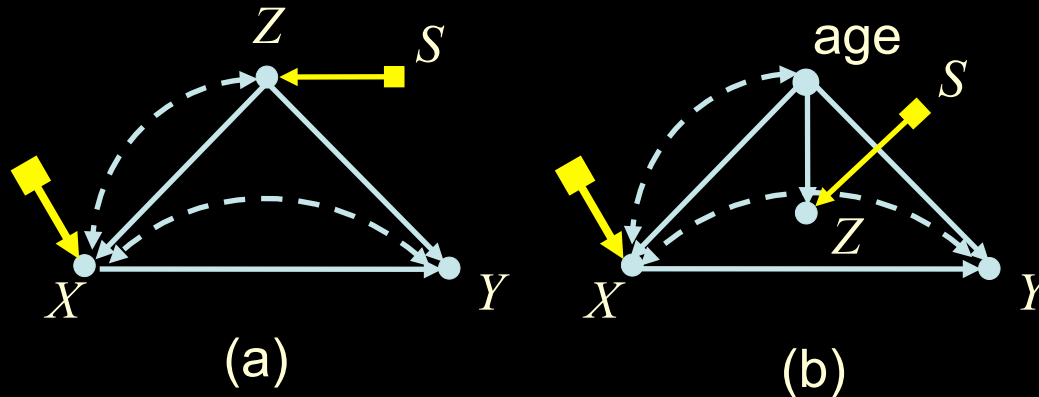
LA:  $P(y | do(x), z)$

Z	X	Y

NYC:  $P^*(x, y, z)$

Z	X	Y

# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS



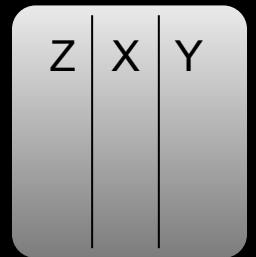
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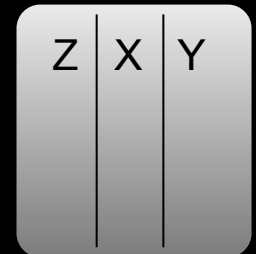
b)  $Z$  represents language skill

$$P^*(y | do(x)) = ?$$

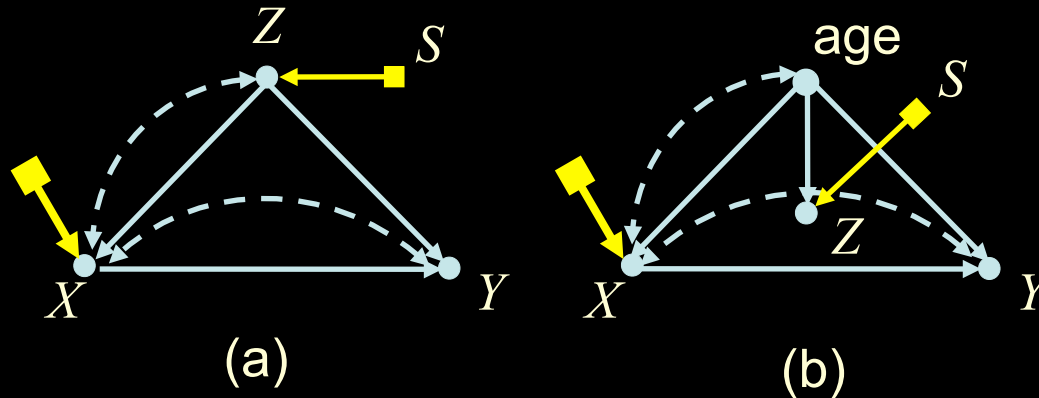
LA:  $P(y | do(x), z)$



NYC:  $P^*(x, y, z)$



# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS



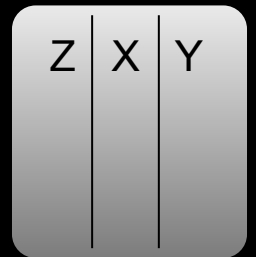
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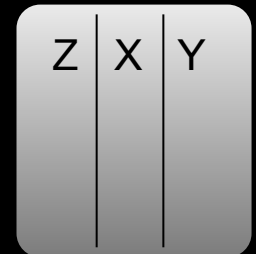
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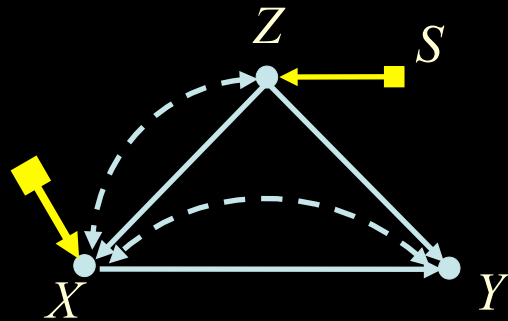
LA:  $P(y | do(x), z)$



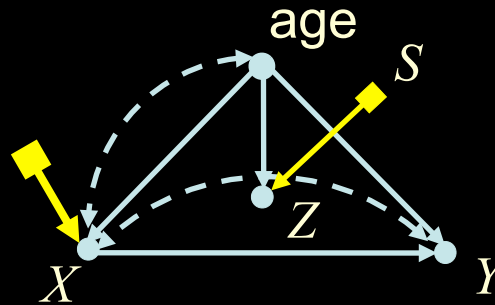
NYC:  $P^*(x, y, z)$



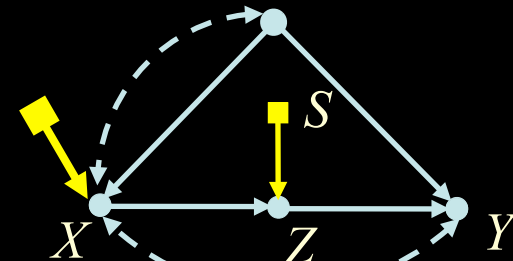
# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS



(a)



(b)



(c)

LA:  $P(y | do(x), z)$

a)  $Z$  represents age

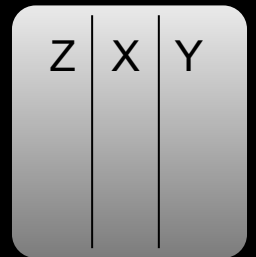
$$P^*(y | do(x)) = \sum_z P(y | do(x), z) P^*(z)$$

b)  $Z$  represents language skill

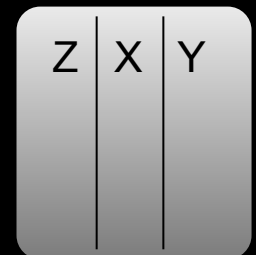
$$P^*(y | do(x)) = P(y | do(x))$$

c)  $Z$  represents a bio-marker

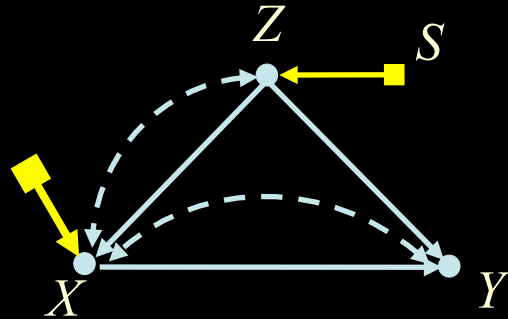
$$P^*(y | do(x)) = ?$$



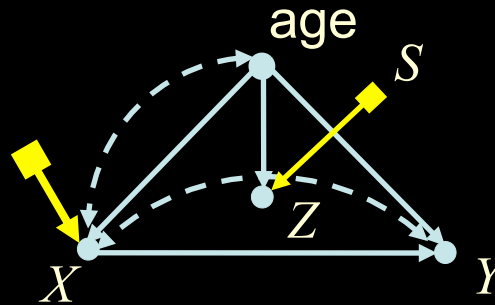
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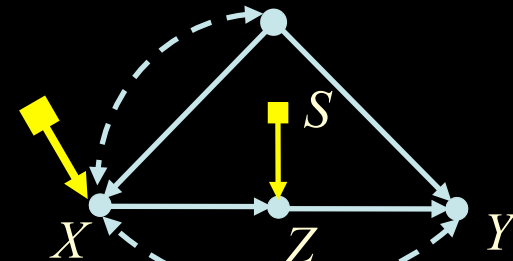
# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS



(a)



(b)

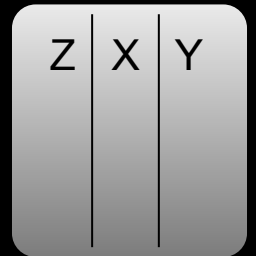


(c)

LA:  $P(y | do(x), z)$

a)  $Z$  represents age

$$P^*(y | do(x)) = \sum_z P(y | do(x), z) P^*(z)$$



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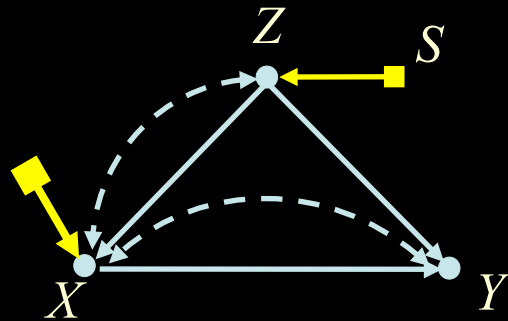
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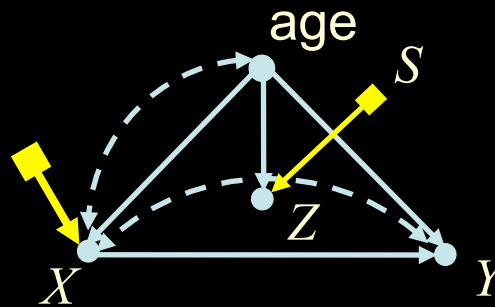
$$P^*(y | do(x)) = \sum_z P(y | do(x), z) P^*(z | x)$$



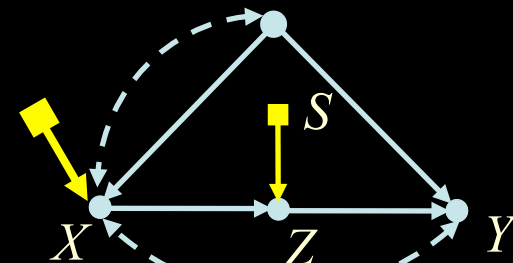
# TRANSPORT FORMULA SENSITIVITY TO THE CAUSAL ASSUMPTIONS



(a)



(b)



(c)

LA:  $P(y | do(x), z)$

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**Lesson.** Causal assumptions are required since the data does not impose enough constraints over the causal structure, and the results are structure-sensitive.

$$P^*(y | do(x)) = \sum_z P(y | do(x), z) P^*(z | x)$$

Z	X	Y
---	---	---

NYC:  $P^*(x, y, z)$

Z	X	Y
---	---	---

# DECISION PROBLEM. IS THE TARGET EFFECT TRANSPORTABLE?

---

## 1 Query

$$Q = P^*(y \mid do(x))$$

# DECISION PROBLEM.

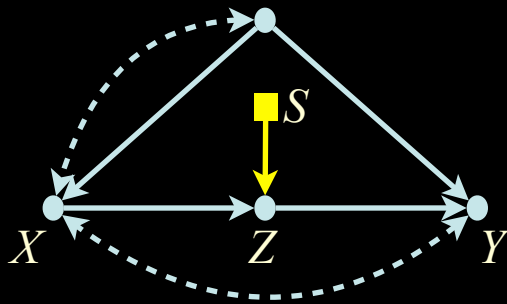
## IS THE TARGET EFFECT TRANSPORTABLE?

---

### 1 Query

$$Q = P^*(y \mid do(x))$$

### 2 Graph





# DECISION PROBLEM.

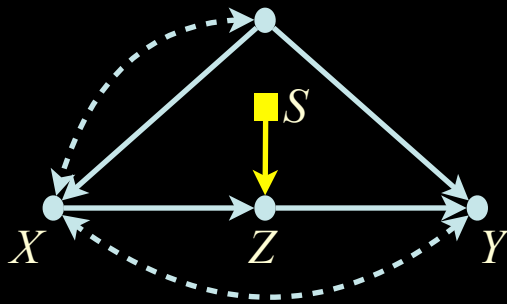
## IS THE TARGET EFFECT TRANSPORTABLE?

---

### 1 Query

$$Q = P^*(y \mid do(x))$$

### 2 Graph



### 3 Data

$$P(x, z, y), P(z, y \mid do(x)), P^*(x, z, y)$$

# DECISION PROBLEM.

## IS THE TARGET EFFECT TRANSPORTABLE?

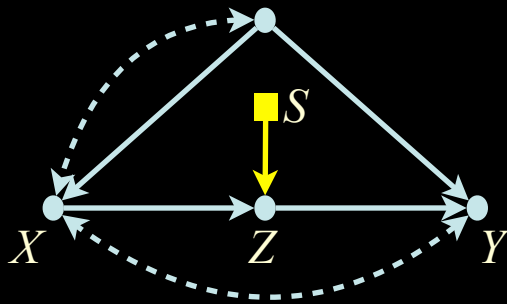
---

Q: Based on the current knowledge about the problem (2) and the available datasets (3), is the research question (1) transportable?

### 1 Query

$$Q = P^*(y \mid do(x))$$

### 2 Graph



### 3 Data

$$P(x, z, y), P(z, y \mid do(x)), P^*(x, z, y)$$

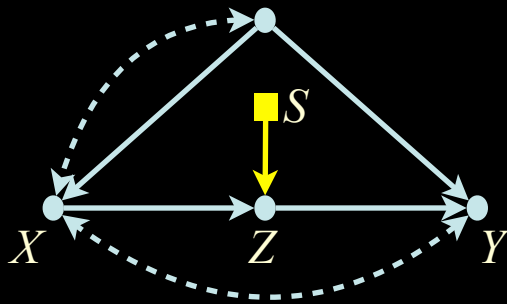
# DECISION PROBLEM.

## IS THE TARGET EFFECT TRANSPORTABLE?

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1 **Query**  
 $Q = P^*(y \mid do(x))$

2 **Graph**



3 **Data**

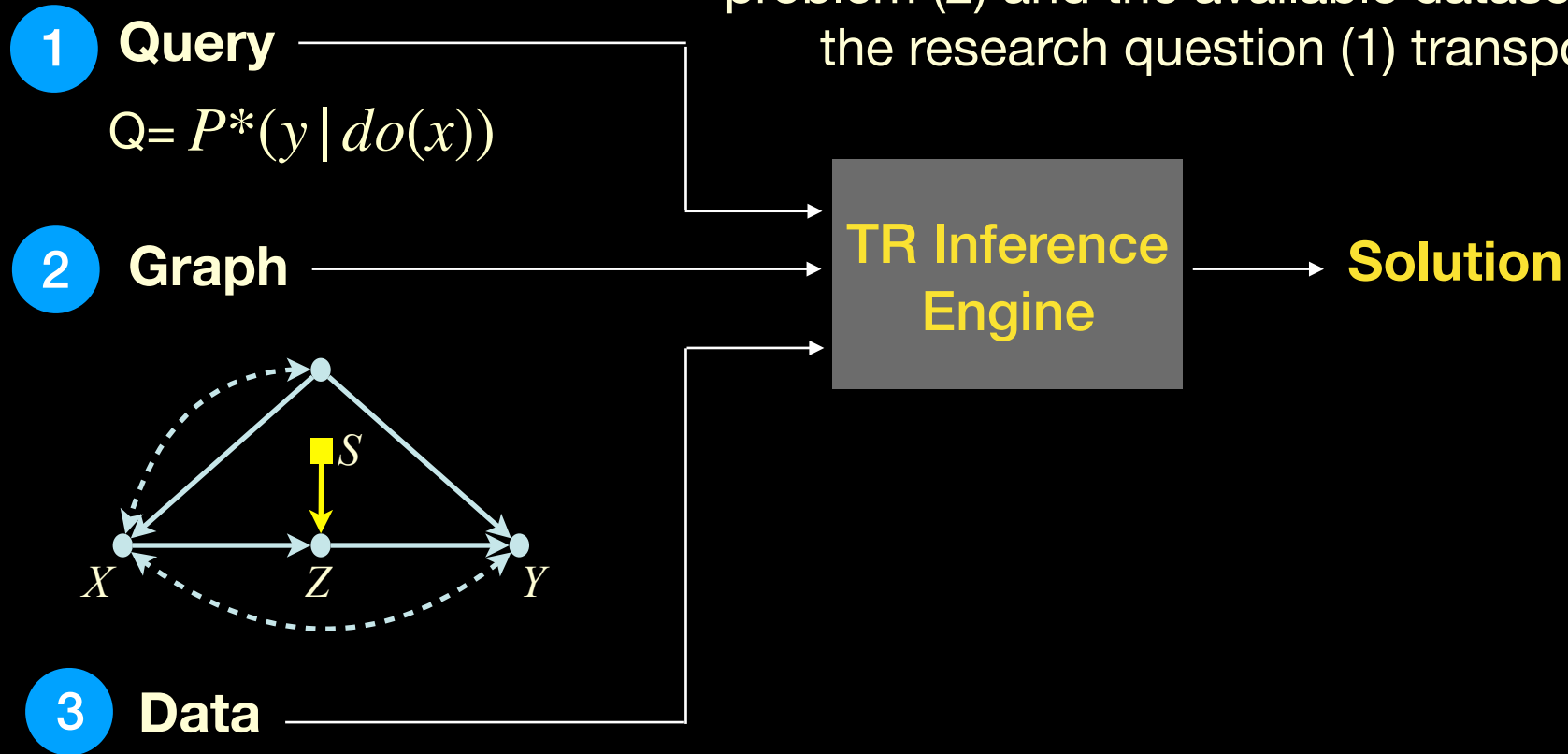
TR Inference Engine

$P(x, z, y), P(z, y \mid do(x)), P^*(x, z, y)$

# DECISION PROBLEM.

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Q: Based on the current knowledge about the problem (2) and the available datasets (3), is the research question (1) transportable?

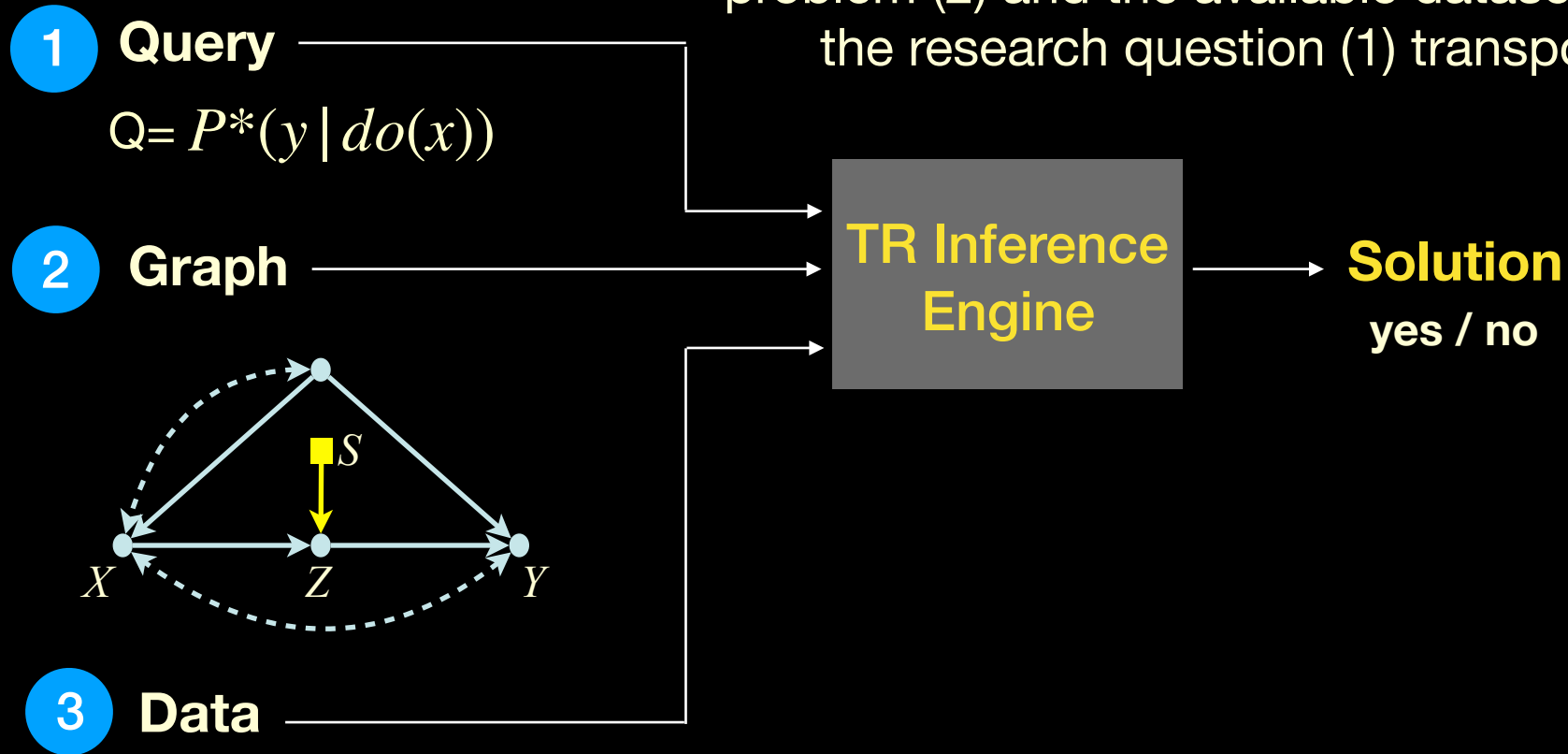


$$P(x, z, y), P(z, y \mid do(x)), P^*(x, z, y)$$

# DECISION PROBLEM.

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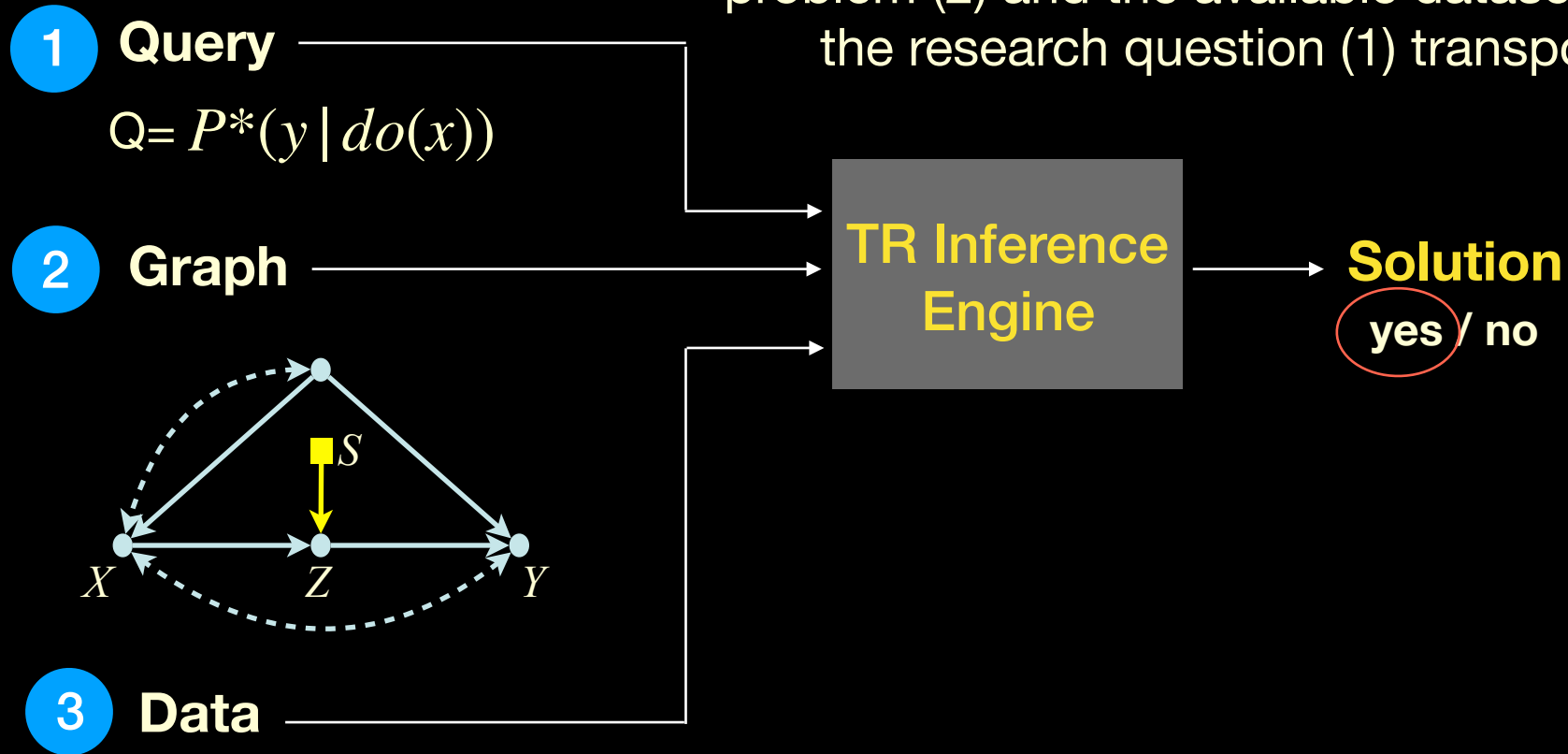


$$P(x, z, y), P(z, y \mid do(x)), P^*(x, z, y)$$

# DECISION PROBLEM.

## IS THE TARGET EFFECT TRANSPORTABLE?

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$$P(x, z, y), P(z, y | do(x)), P^*(x, z, y)$$

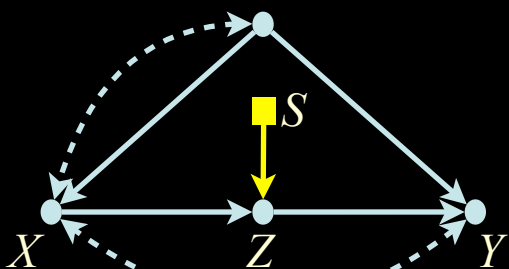
# DECISION PROBLEM.

## IS THE TARGET EFFECT TRANSPORTABLE?

Q: Based on the current knowledge about the problem (2) and the available datasets (3), is the research question (1) transportable?

**1 Query**  
 $Q = P^*(y | do(x))$

**2 Graph**



**3 Data**

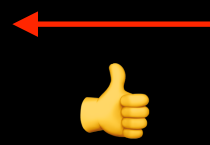
**TR Inference Engine**

**Solution**  
 yes / no

$$P^*(y | do(x)) = \sum_z P(y | do(x), z) P^*(z | x)$$

Causation in target domain  
 (Query)

Obs. Data in target +  
 Exp. Data in source  
 (Data)



$$P(x, z, y), P(z, y | do(x)), P^*(x, z, y)$$

# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

---

**Thm:** A causal quantity  $Q$  is transportable from  $\Pi$  to  $\Pi^*$  ( $G$ ) **if and only if** there exists a do-calculus reduction of  $Q(\Pi^*)$  to an estimand that is a function of the observed distributions.

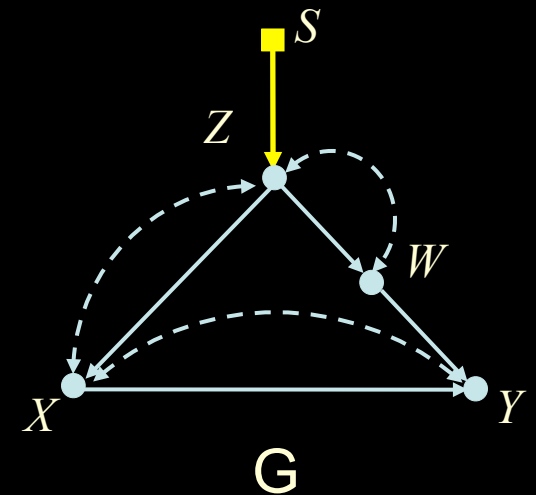


# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

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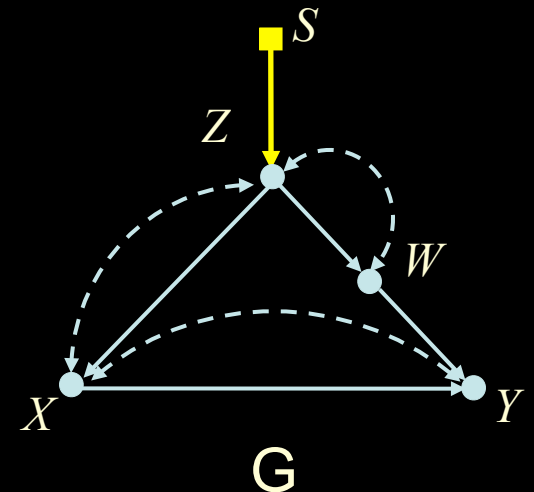


# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

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$Q = P^*(y \mid \text{do}(x))$  query



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$Q = P^*(y \mid \text{do}(x))$  query

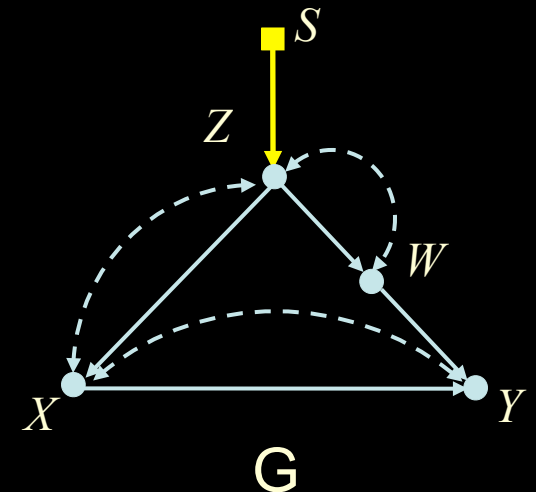
$$= P(y \mid \text{do}(x), s)$$

$$= \sum_w P(y \mid \text{do}(x), s, w) P(w \mid \text{do}(x), s)$$

$$= \sum_w P(y \mid \text{do}(x), w) P(w \mid \text{do}(x), s)$$

$$= \sum_w P(y \mid \text{do}(x), w) P(w \mid s)$$

$$= \sum_w P(y \mid \text{do}(x), w) P^*(w)$$



# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

**Thm:** A causal quantity  $Q$  is transportable from  $\Pi$  to  $\Pi^*$  ( $G$ ) if and only if there exists a do-calculus reduction of  $Q(\Pi^*)$  to an estimand that is a function of the observed distributions.

$$Q = P^*(y \mid \text{do}(x)) \quad \text{query}$$

$$= P(y \mid \text{do}(x), s)$$

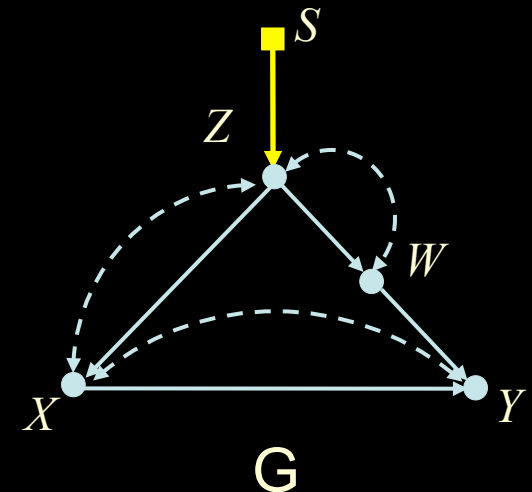
$$= \sum_w P(y \mid \text{do}(x), s, w) P(w \mid \text{do}(x), s)$$

$$= \sum_w P(y \mid \text{do}(x), w) P(w \mid \text{do}(x), s)$$

$$= \sum_w P(y \mid \text{do}(x), w) P(w \mid s)$$

$$= \sum_w P(y \mid \text{do}(x), w) P^*(w)$$

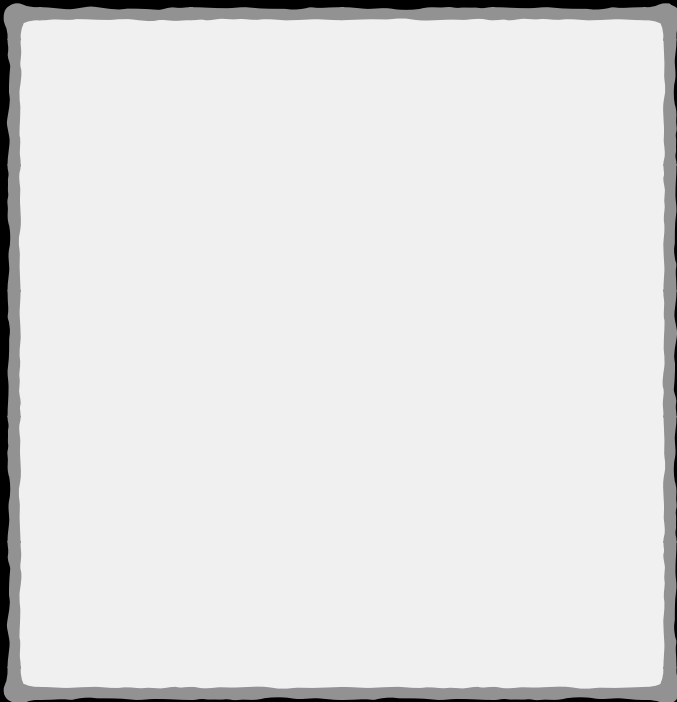
data



# MEANING OF TRANSPORTABILITY

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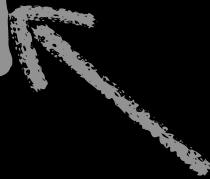
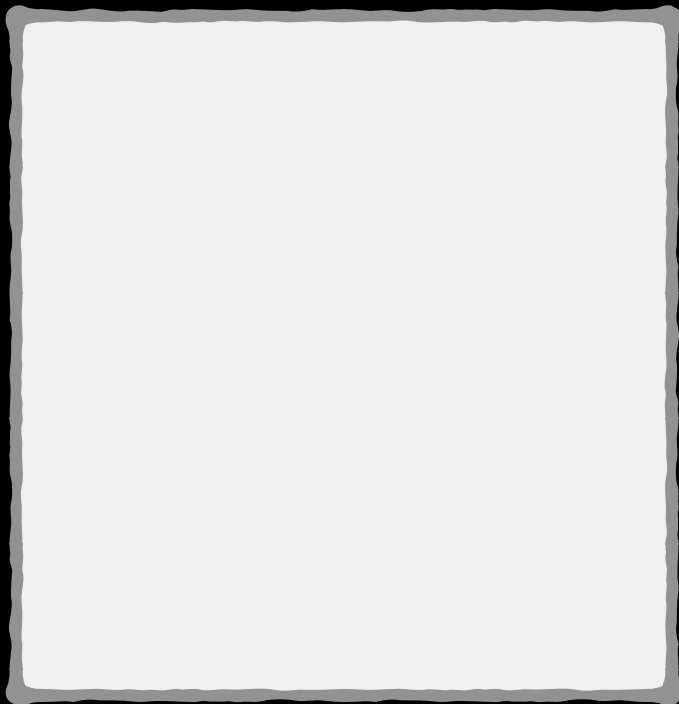
$P^*(y|do(x))$  is  
transportable in  $G$



# MEANING OF TRANSPORTABILITY

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$P^*(y|do(x))$  is  
transportable in  $G$

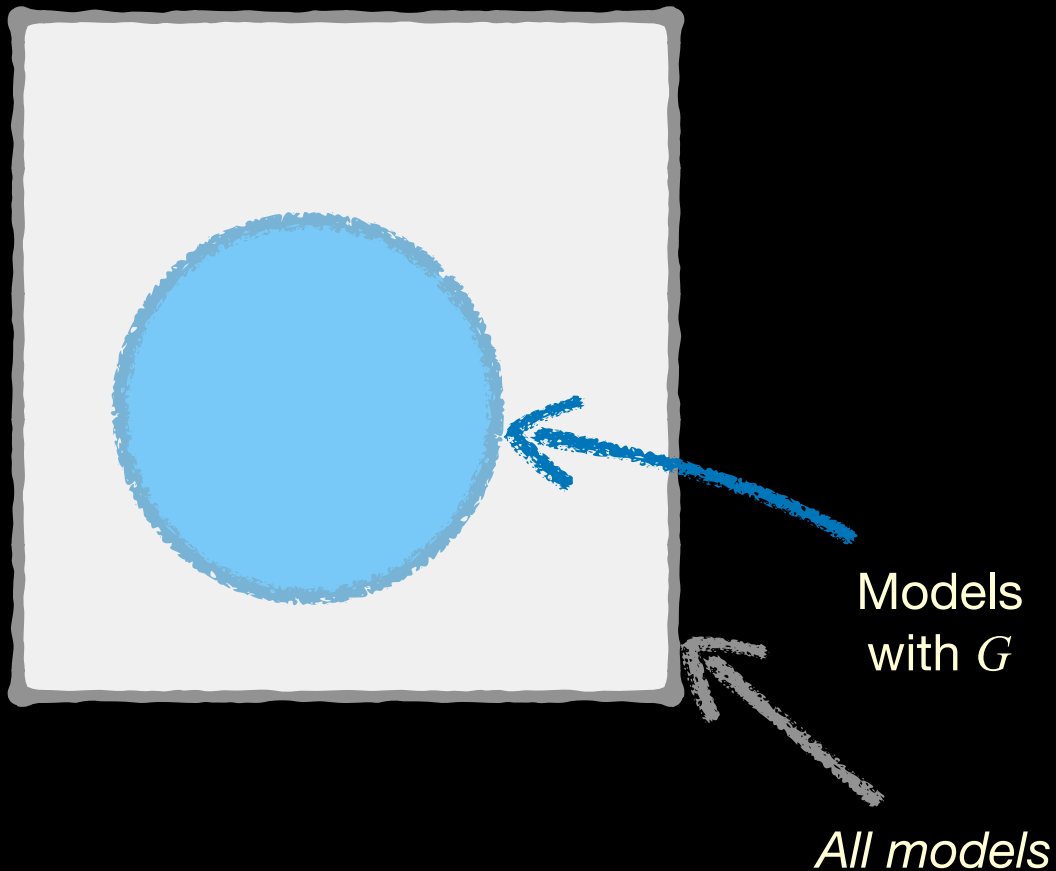


*All models*

# MEANING OF TRANSPORTABILITY

---

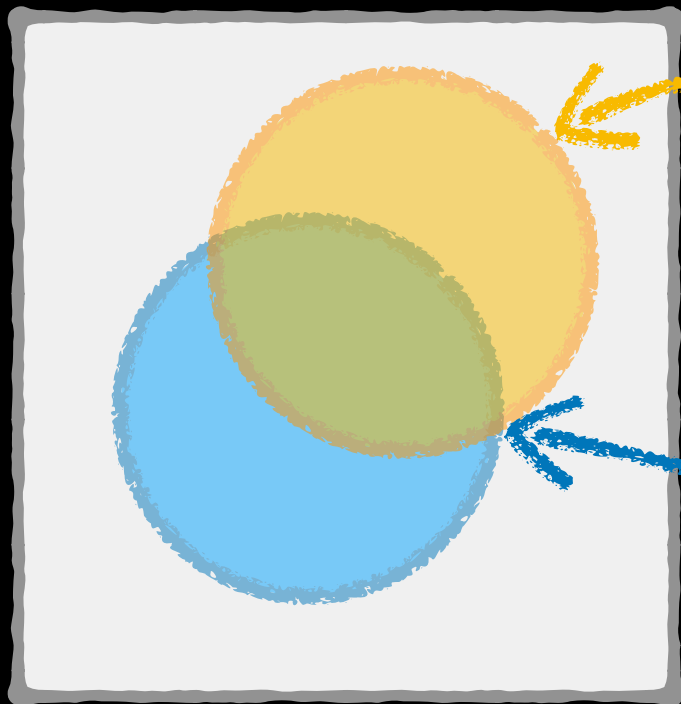
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# MEANING OF TRANSPORTABILITY

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$P^*(y|do(x))$  is  
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Models  
inducing  
 $P(v), P^*(v),$   
 $P(v|do(x))$

Models  
with  $G$

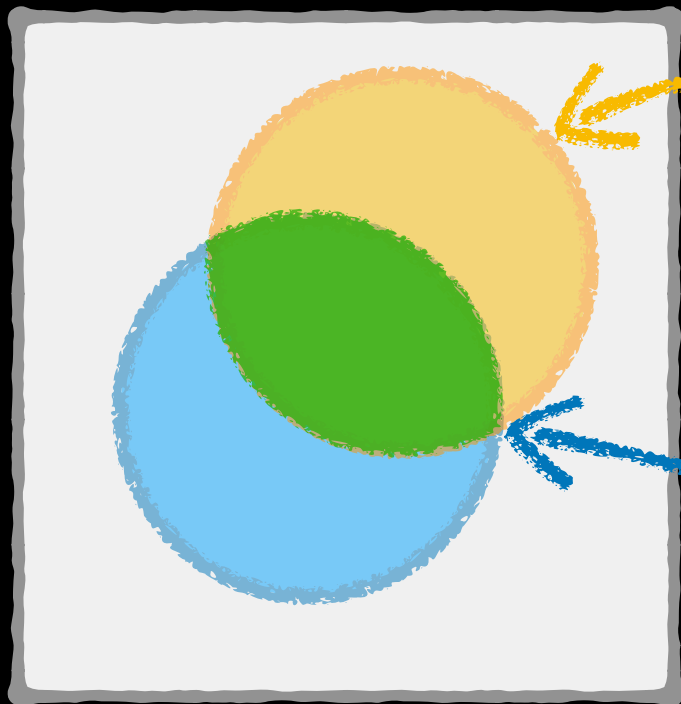
All models



# MEANING OF TRANSPORTABILITY

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$P^*(y|do(x))$  is  
transportable in  $G$



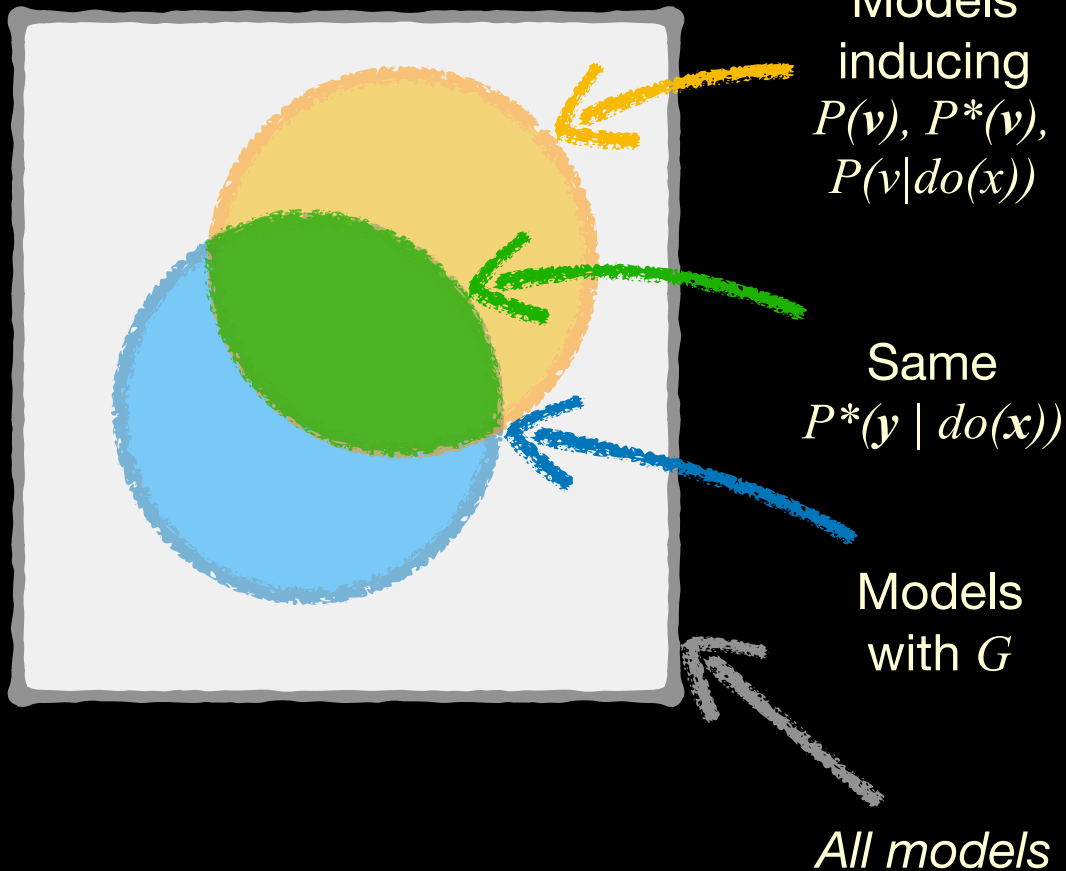
Models  
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 $P(v)$ ,  $P^*(v)$ ,  
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Models  
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All models

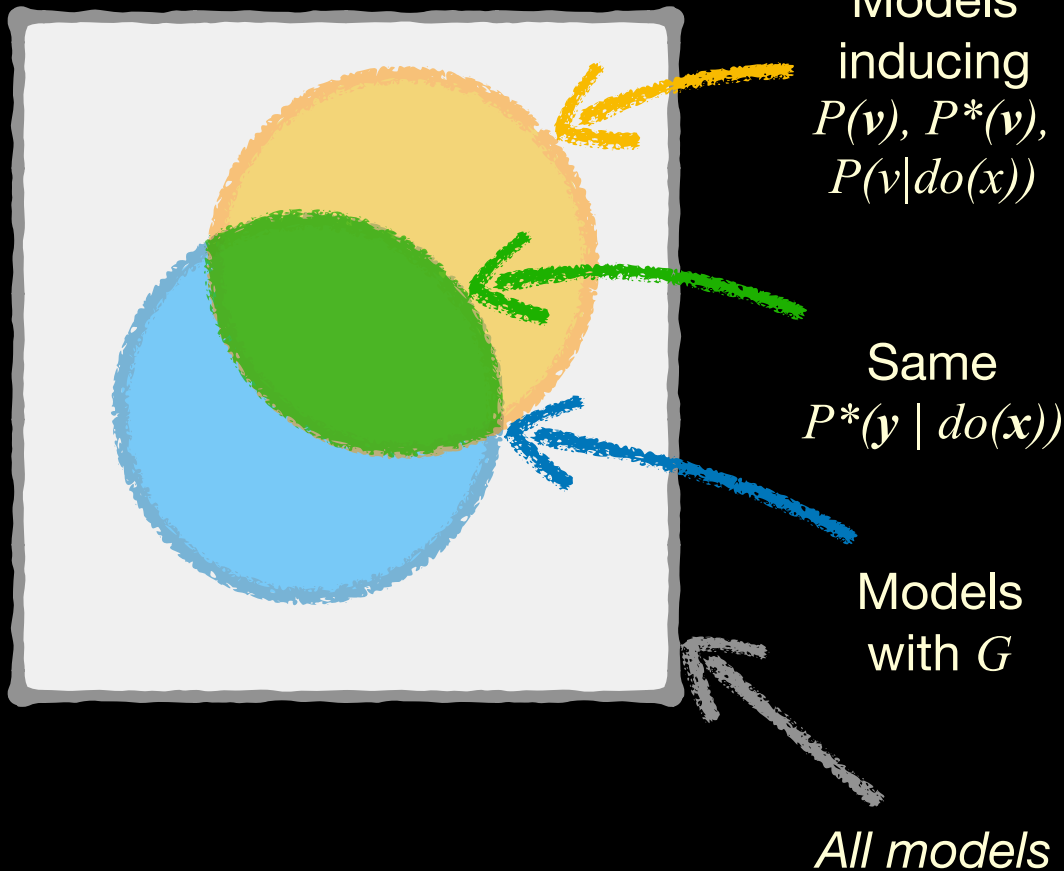
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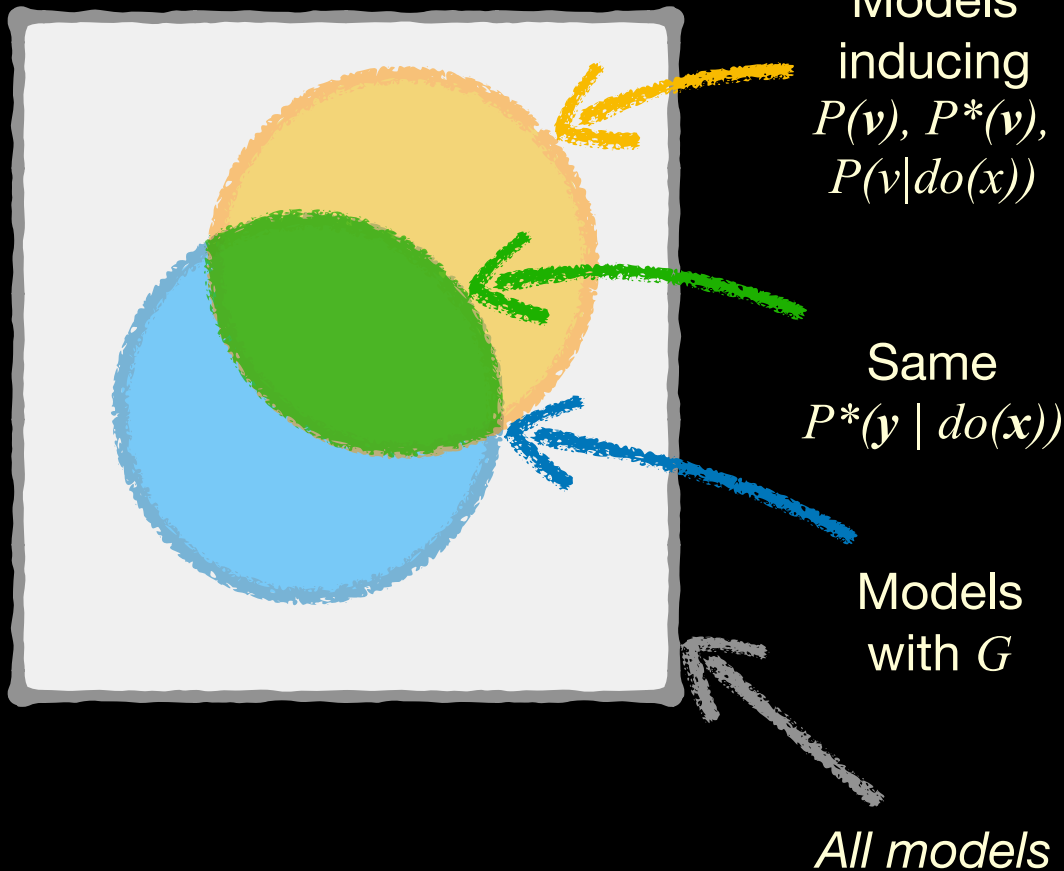
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Formally,  
for any two causal models (encoding the unobserved nature),  $N_1, N_2$ , s.t.

# MEANING OF TRANSPORTABILITY

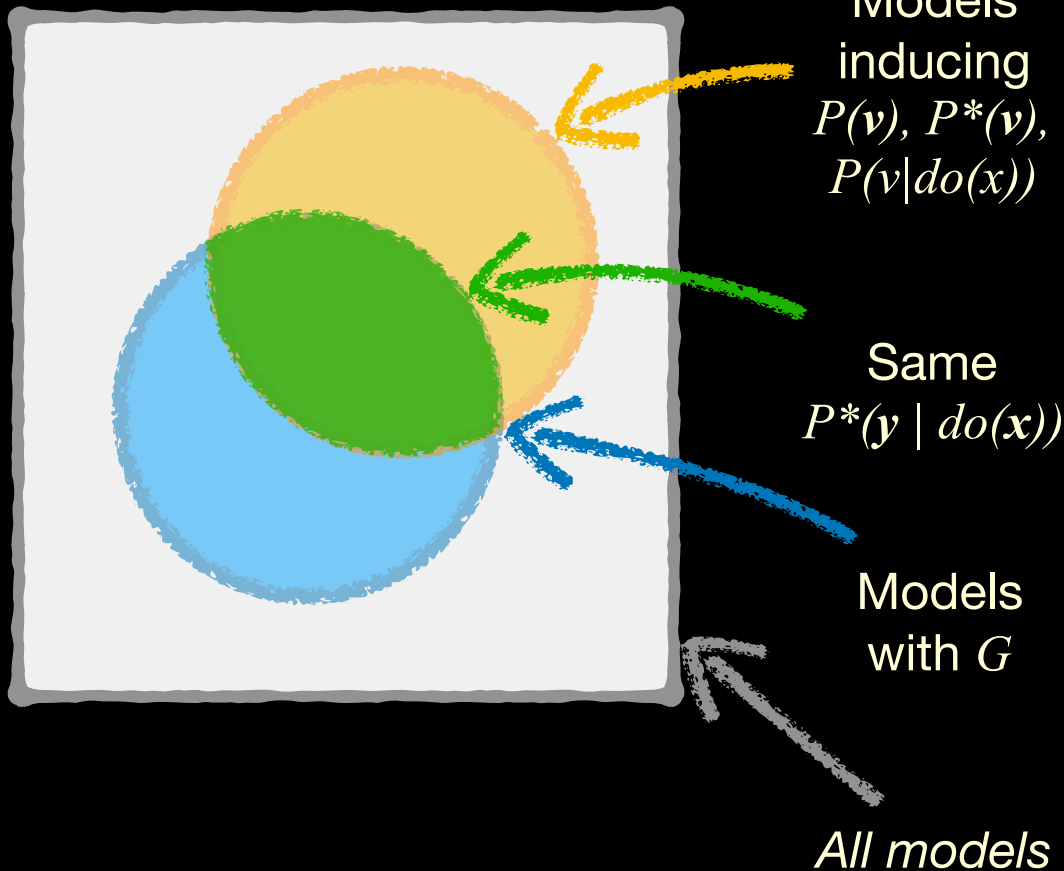
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 $G(N_1) = G(N_2) = G$ ,

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$P^*(y|do(x))$  is transportable in  $G$



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$$G(N_1) = G(N_2) = G,$$

$$P_1(v) = P_2(v),$$

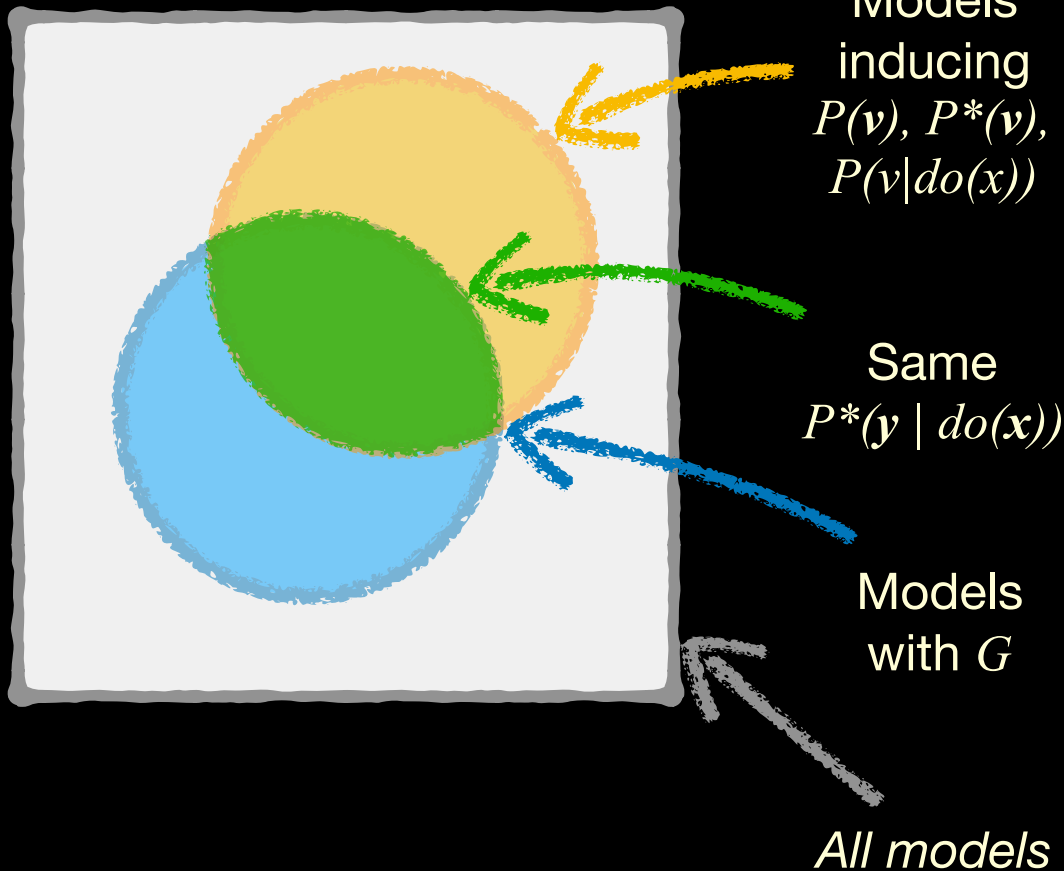
$$P^*_1(v) = P^*_2(v),$$

$$P_1(v | do(x)) =$$

$$P_2(v | do(x))$$

# MEANING OF TRANSPORTABILITY

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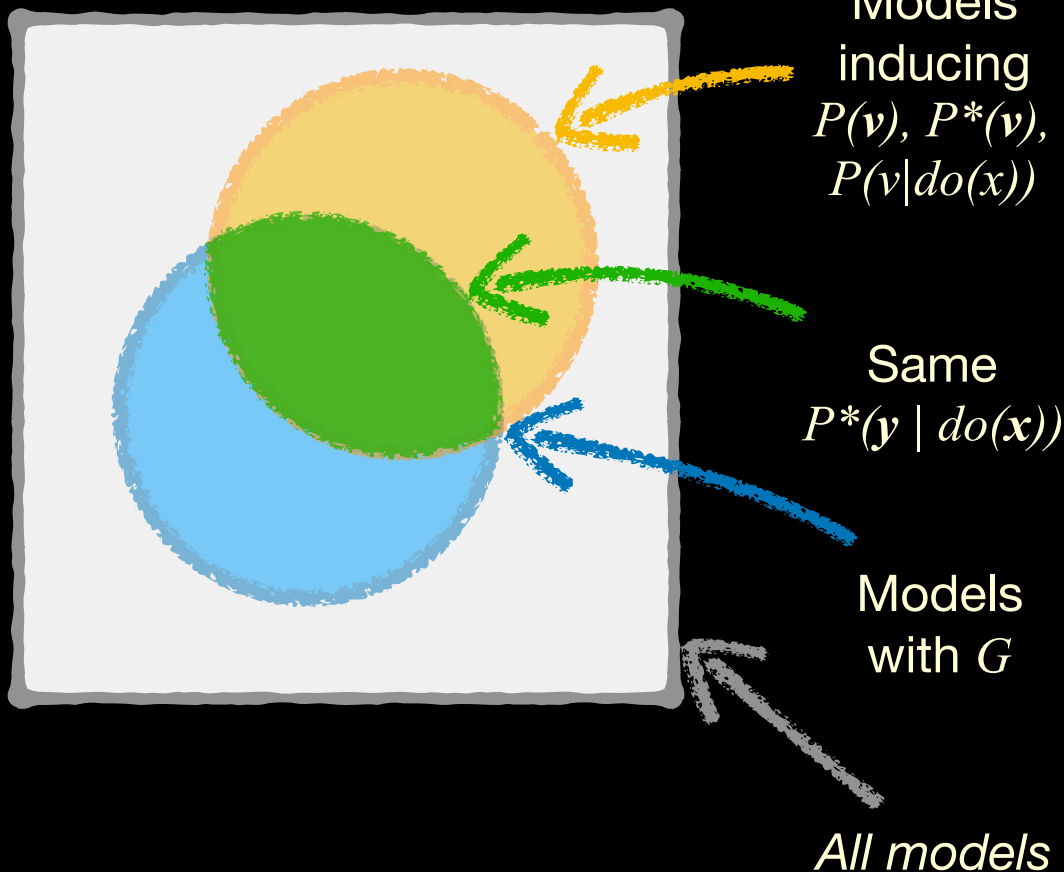
$$P_2(v | do(x)), \text{ then}$$

$$P^*_1(y | do(x)) =$$

$$P^*_2(y | do(x)).$$

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$$P_2(v | do(x)), \text{ then}$$

$$P^*_1(y | do(x)) =$$

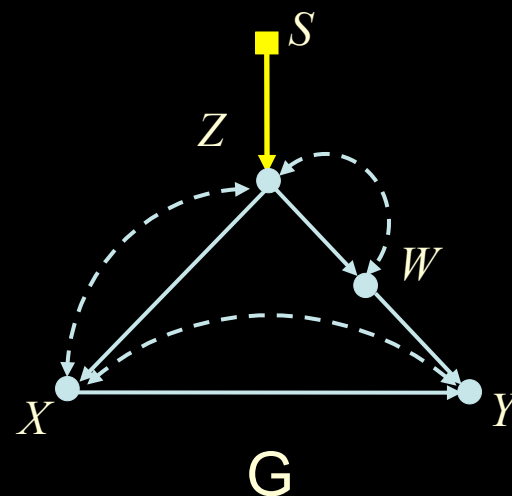
$$P^*_2(y | do(x)).$$

# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

---

**Thm:** A causal quantity  $Q$  is transportable from  $\Pi$  to  $\Pi^*$  ( $G$ ) if and only if there exists a do-calculus reduction of  $Q(\Pi^*)$  to an estimand that is a function of the observed distributions.

$$Q = P^*(y \mid \text{do}(x)) = ?$$



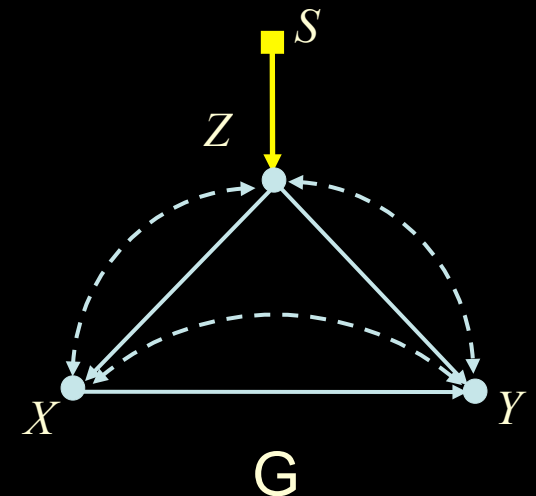


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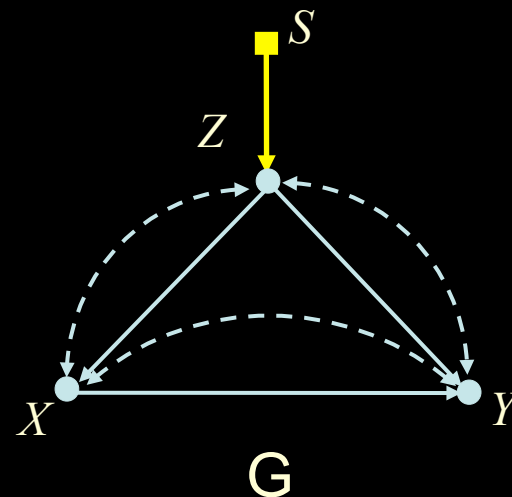


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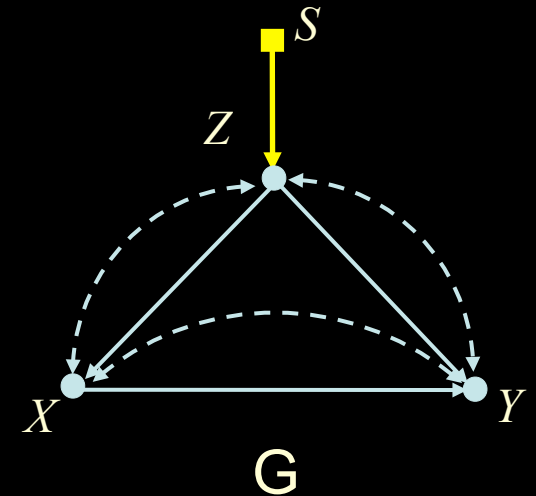


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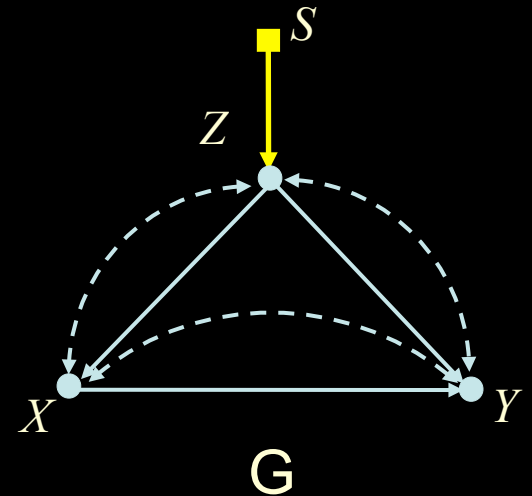
# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

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Proof.  $\exists N_1, N_2$



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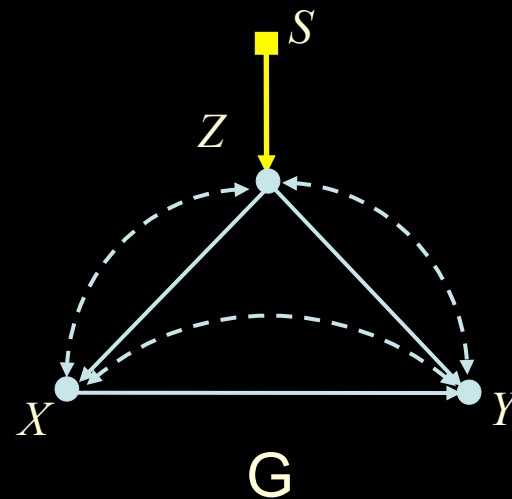
$Q = P^*(y \mid \text{do}(x)) = ?$  Nope.

Proof.  $\exists N_1, N_2$

$N_1$

$$\begin{cases} Z \leftarrow U_{zy} \vee (S \wedge U_{xz}) \\ X \leftarrow Z \oplus U_{xy} \\ Y \leftarrow U_y \end{cases}$$

$$P(u_i) = 1/2$$

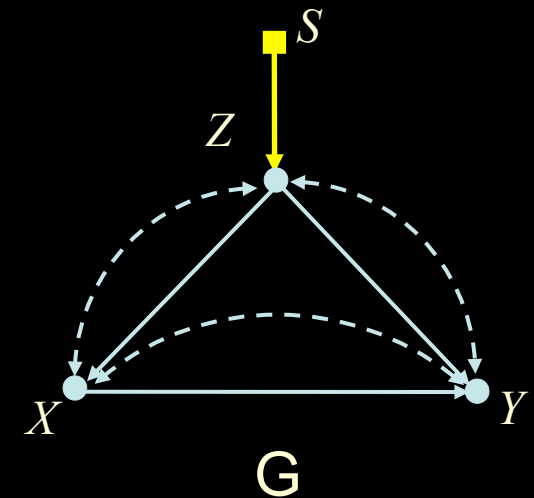


# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

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$$\begin{cases} Z \leftarrow U_{zy} \vee (S \wedge U_{xz}) \\ X \leftarrow Z \oplus U_{xy} \\ Y \leftarrow ((X \oplus Z \oplus U_{xy}) \wedge (Z \oplus U_{zy})) \vee U_y \end{cases}$$

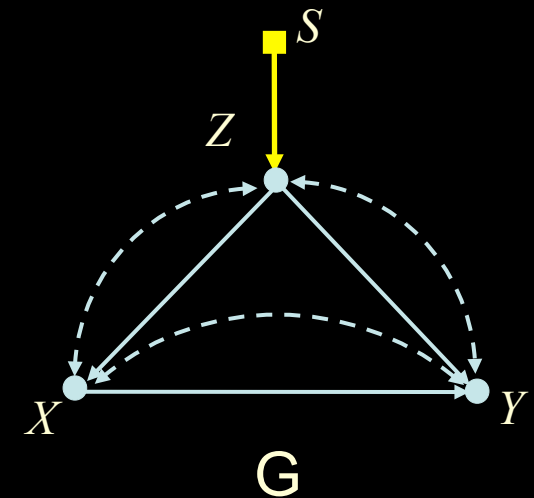
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$Q = P^*(y \mid \text{do}(x)) = ?$  Nope.

Proof.  $\exists N_1, N_2$  s.t.  $G(N_1) = G(N_2) = G$ ,



$N_1$

$$\begin{cases} Z \leftarrow U_{zy} \vee (S \wedge U_{xz}) \\ X \leftarrow Z \oplus U_{xy} \\ Y \leftarrow U_y \end{cases}$$

$$P(u_i) = 1/2$$

$N_2$

$$\begin{cases} Z \leftarrow U_{zy} \vee (S \wedge U_{xz}) \\ X \leftarrow Z \oplus U_{xy} \\ Y \leftarrow ((X \oplus Z \oplus U_{xy}) \wedge (Z \oplus U_{zy})) \vee U_y \end{cases}$$

$$P(u_i) = 1/2$$

# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

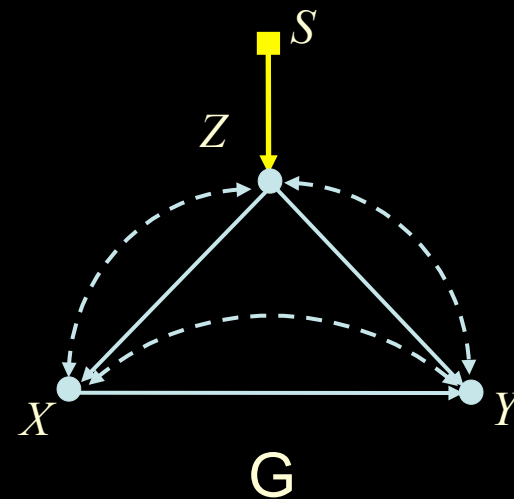
**Thm:** A causal quantity  $Q$  is transportable from  $\Pi$  to  $\Pi^*$  ( $G$ ) if and only if there exists a do-calculus reduction of  $Q(\Pi^*)$  to an estimand that is a function of the observed distributions.

$Q = P^*(y \mid \text{do}(x)) = ?$  Nope.

Proof.  $\exists N_1, N_2$  s.t.  $G(N_1) = G(N_2) = G$ ,

$P^*_1(z,x,y) = P^*_2(z,x,y)$ ,  $P_1(z,x,y) = P_2(z,x,y)$ ,

$P_1(z,y \mid \text{do}(x)) = P_2(z,y \mid \text{do}(x))$ , but



$N_1$

$$\begin{cases} Z \leftarrow U_{zy} \vee (S \wedge U_{xz}) \\ X \leftarrow Z \oplus U_{xy} \\ Y \leftarrow U_y \end{cases}$$

$$P(u_i) = 1/2$$

$N_2$

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# RESULT 1: SYNTACTIC CHARACTERIZATION OF TRANSPORTABILITY

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$Q = P^*(y \mid \text{do}(x)) = ?$  Nope.

Proof.  $\exists N_1, N_2$  s.t.  $G(N_1) = G(N_2) = G$ ,

$P^*_1(z, x, y) = P^*_2(z, x, y)$ ,  $P_1(z, x, y) = P_2(z, x, y)$ ,

$P_1(z, y \mid \text{do}(x)) = P_2(z, y \mid \text{do}(x))$ , but

$P^*_1(y \mid \text{do}(x)) \neq P^*_2(y \mid \text{do}(x))$ .

$N_1$

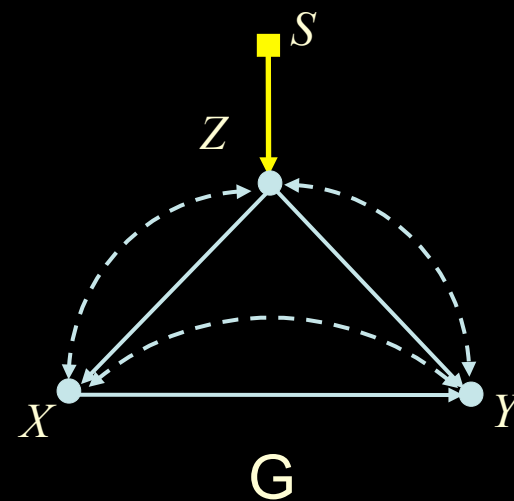
$$\begin{cases} Z \leftarrow U_{zy} \vee (S \wedge U_{xz}) \\ X \leftarrow Z \oplus U_{xy} \\ Y \leftarrow U_y \end{cases}$$

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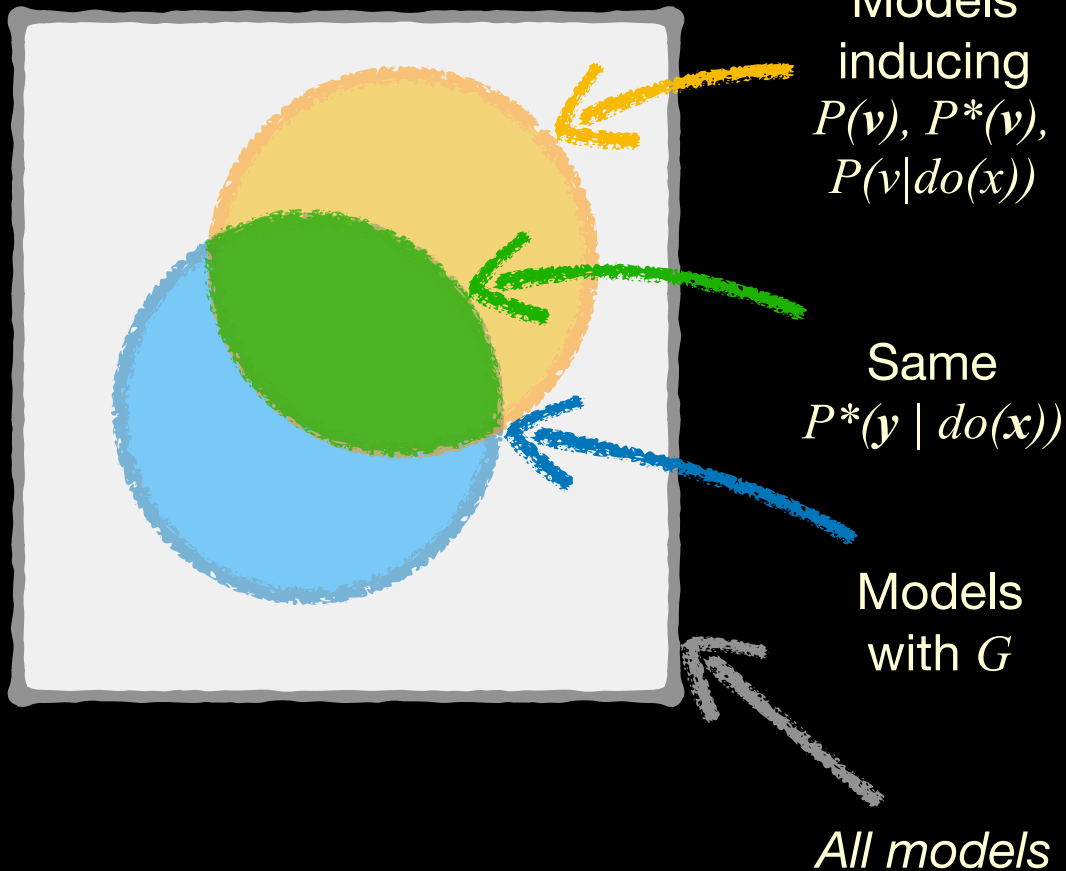
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# MEANING OF TRANSPORTABILITY

---

$P^*(y|do(x))$  is  
transportable in  $G$



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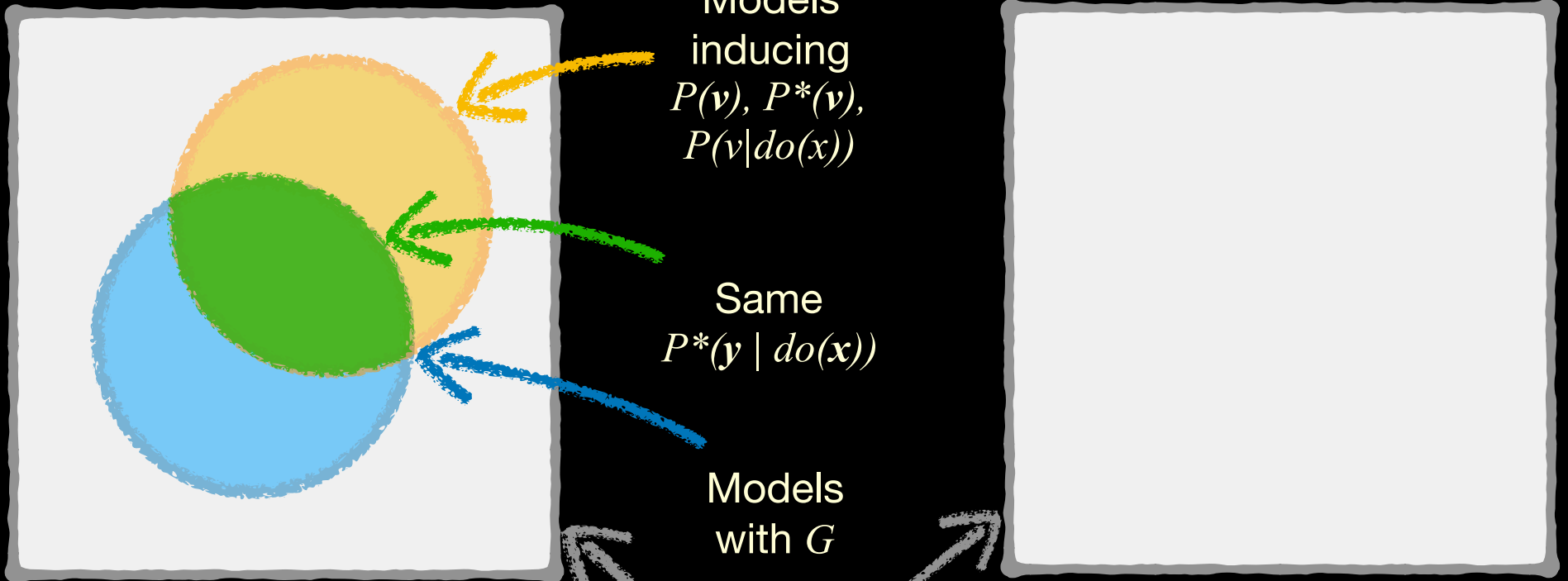
$P^*(y|do(x))$  is  
**not transportable** in  $G$

Models  
inducing  
 $P(\mathbf{v}), P^*(\mathbf{v}),$   
 $P(\mathbf{v}|do(x))$

Same  
 $P^*(y | do(x))$

Models  
with  $G$

All models



# MEANING OF TRANSPORTABILITY

$P^*(y|do(x))$  is  
transportable in  $G$

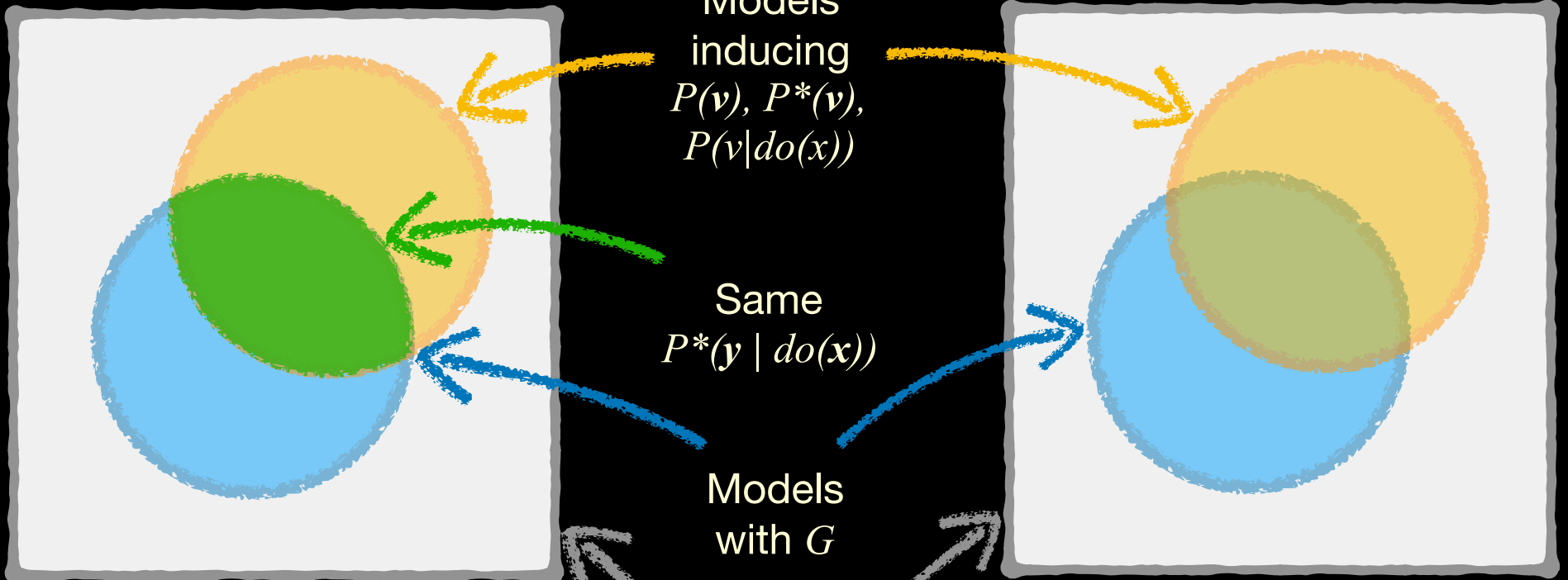
$P^*(y|do(x))$  is  
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Models  
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 $P^*(y | do(x))$

Models  
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All models



# MEANING OF TRANSPORTABILITY

$P^*(y|do(x))$  is  
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$P^*(y|do(x))$  is  
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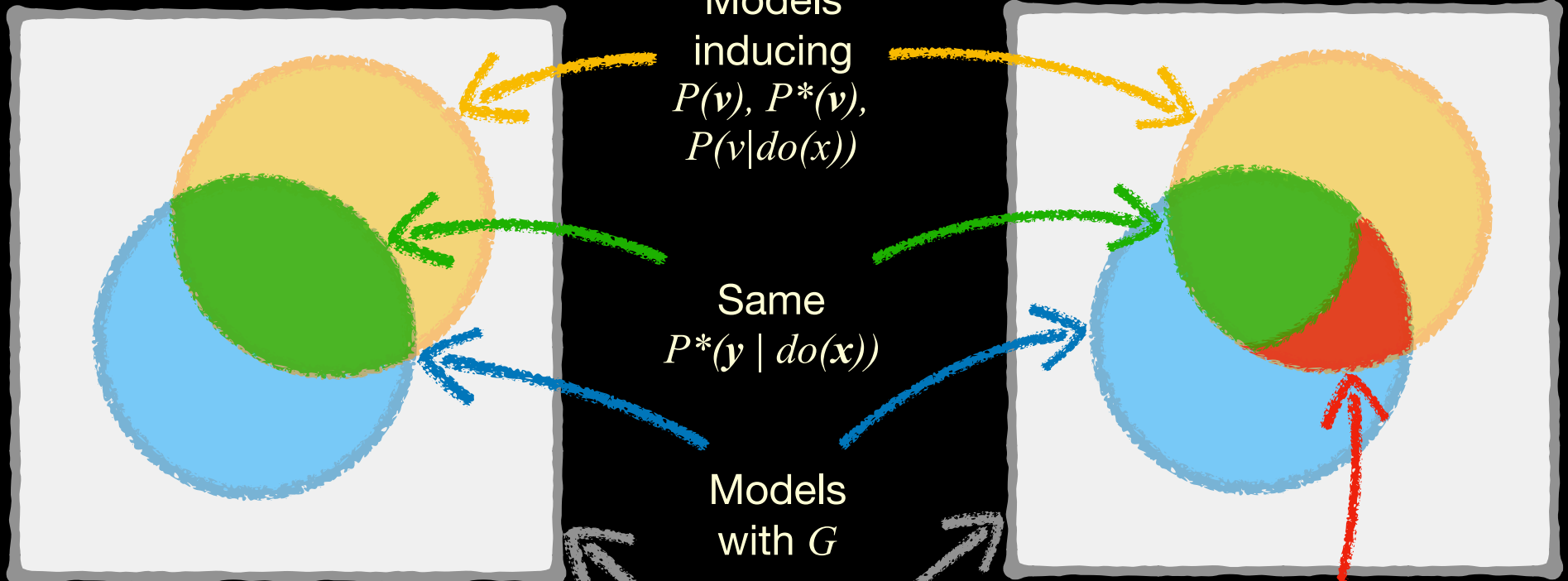
Models  
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Models  
with  $G$

All models

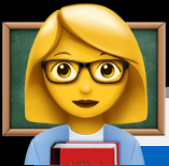
Different  
 $P^*(y | do(x))$  !



# MEANING OF TRANSPORTABILITY

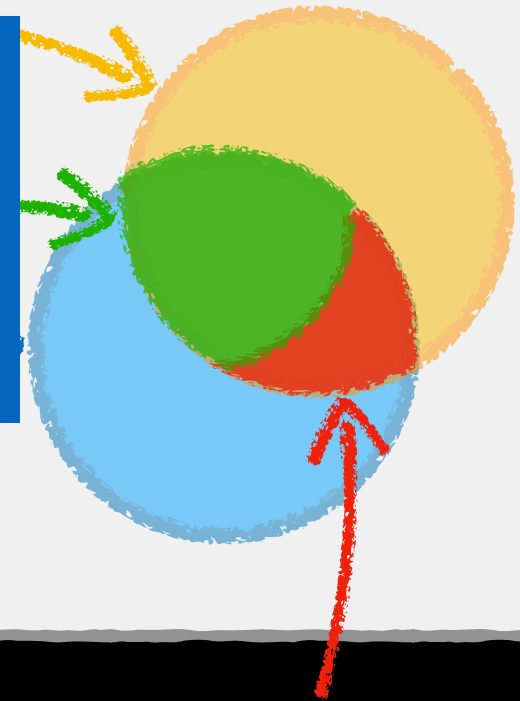
$P^*(y|do(x))$  is transportable in  $G$

$P^*(y|do(x))$  is not transportable in  $G$



Models inducing

**Lesson.** No claim about the target effect can be made in the target (*a la* CLT) regardless of how much data of the observed distributions are collected.



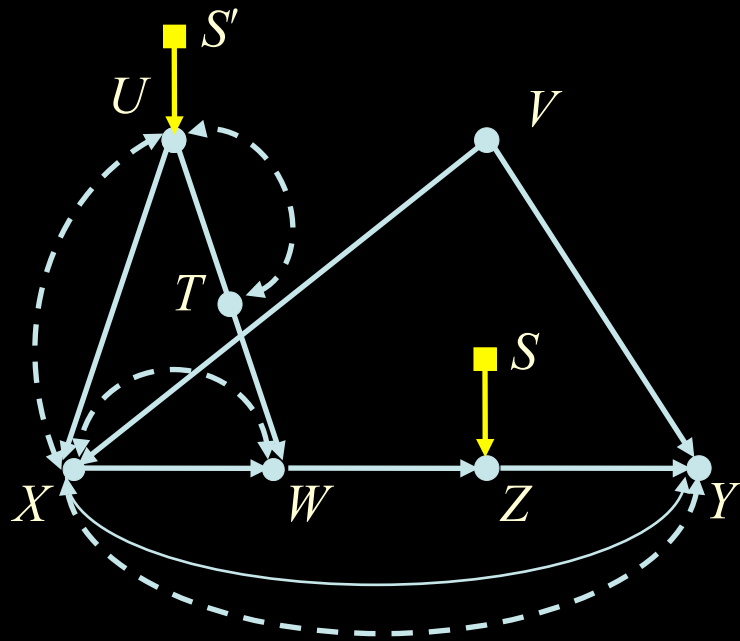
Models with  $G$

All models

Different  $P^*(y | do(x))$  !

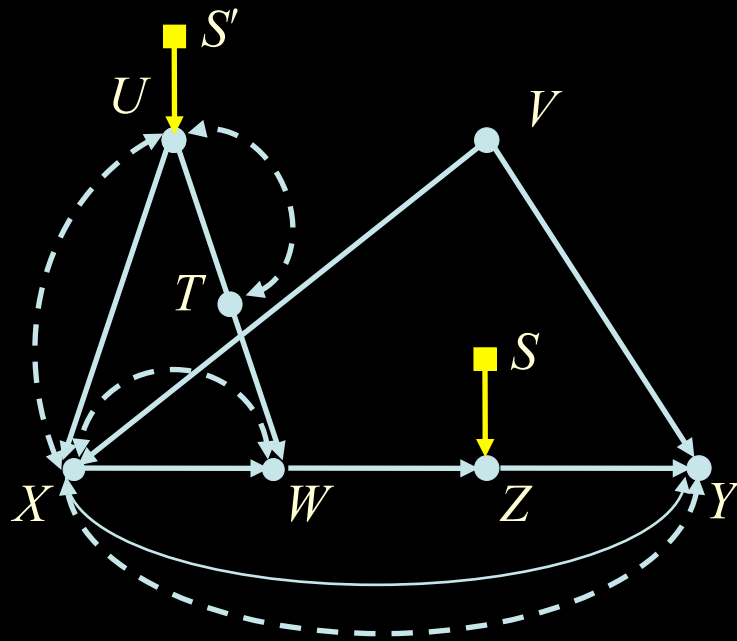
# RESULT 2: ALGORITHM TO DECIDE IF AN EFFECT IS TRANSPORTABLE

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---



INPUT: Annotated Causal Graph

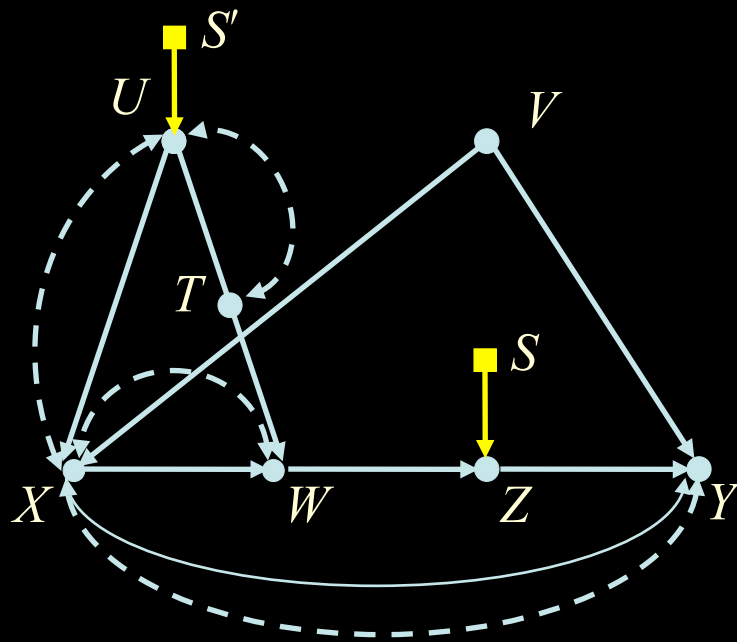
$S$   Factors representing differences

OUTPUT:

1. Transportable or not?
2. Yes = Transport formula
  1. Measurements to be taken in the experimental domain
  2. Measurements to be taken in the target domain
3. No = Not possible



# RESULT 2: ALGORITHM TO DECIDE IF AN EFFECT IS TRANSPORTABLE



INPUT: Annotated Causal Graph

$S$   $\rightarrow$  Factors representing differences

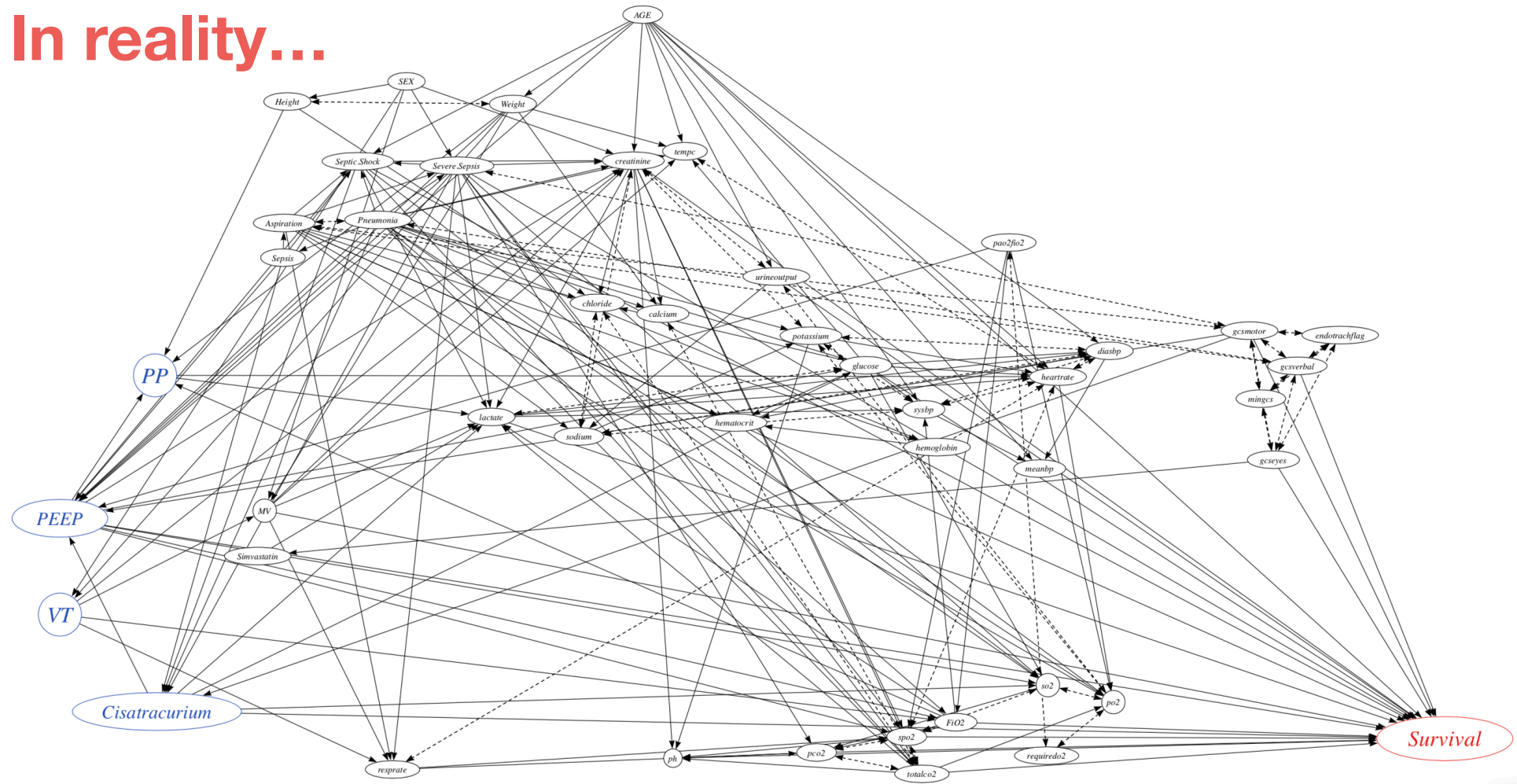
OUTPUT:

1. Transportable or not?
2. Yes = Transport formula
  1. Measurements to be taken in the experimental domain
  2. Measurements to be taken in the target domain
3. No = Not possible

$$P^*(y | do(x)) = \sum_z P(y | do(x), z) \sum_w P^*(z | w) \sum_t P(w | do(x), t) P^*(t)$$

# RESULT 2: ALGORITHM TO DECIDE IF AN EFFECT IS TRANSPORTABLE

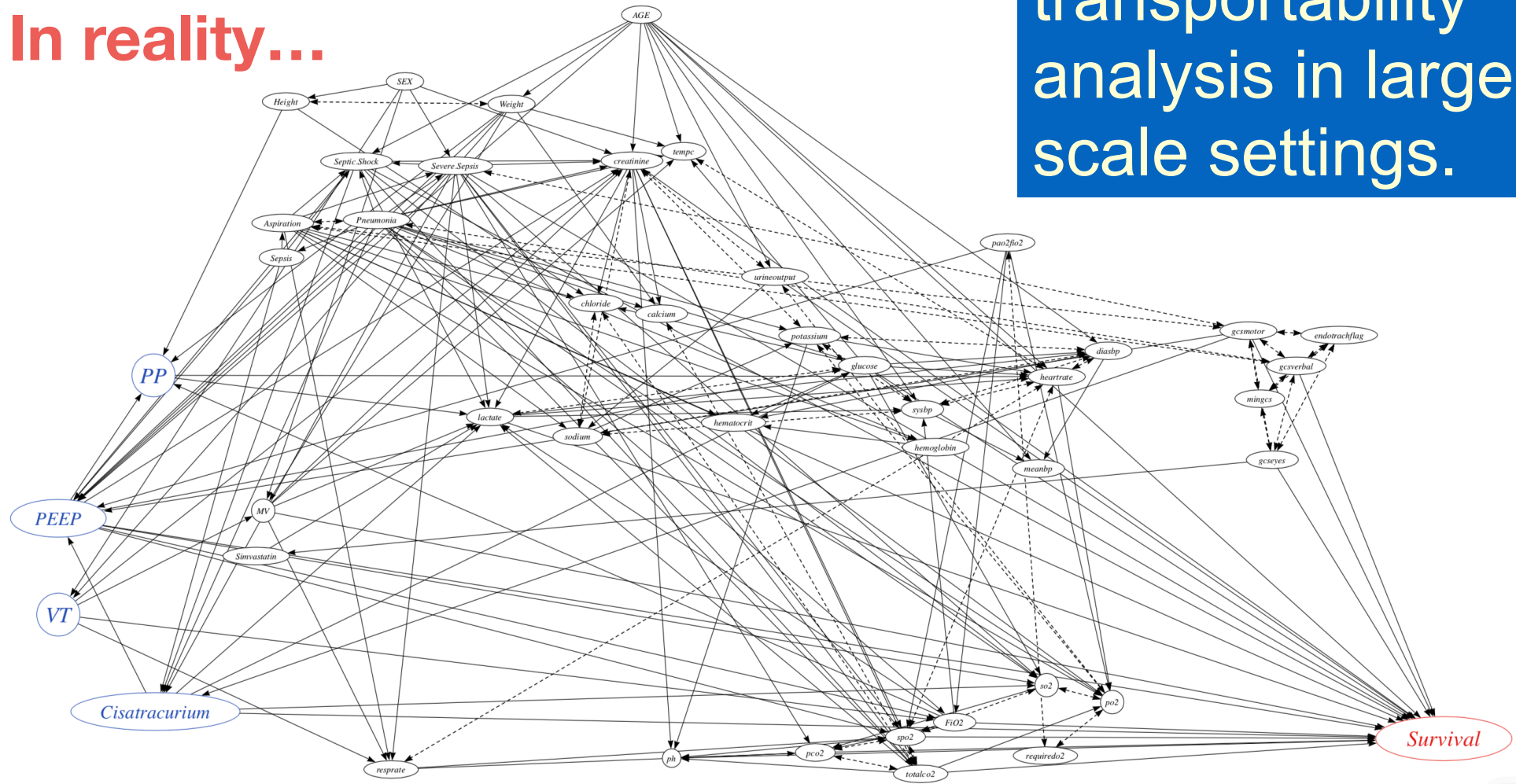
In reality...



# RESULT 2: ALGORITHM TO DECIDE IF AN EFFECT IS TRANSPORTABLE

Result:  
- automated transportability analysis in large-scale settings.

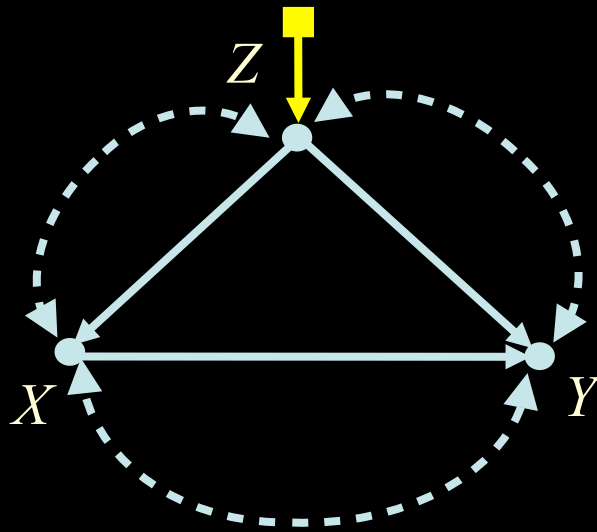
In reality...



# IS THE GOLD STANDARD GOLDEN? (GENERALIZABILITY FROM CLINICAL TRIALS)

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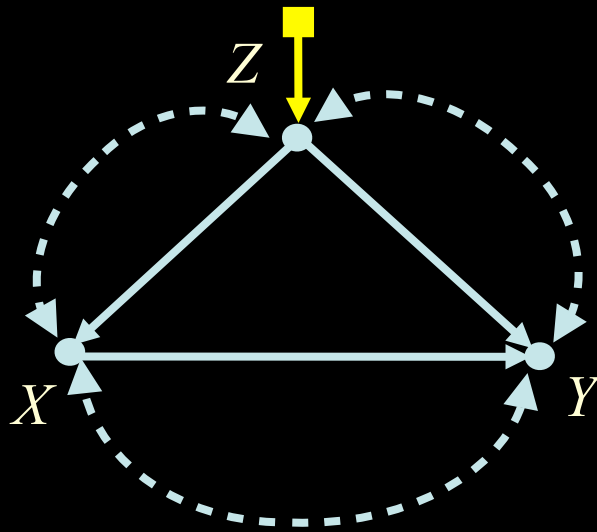
Before randomization



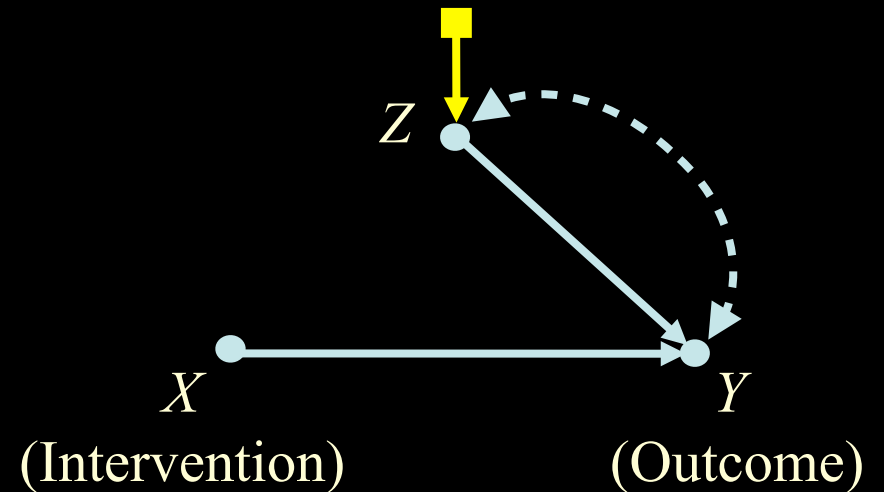
# IS THE GOLD STANDARD GOLDEN? (GENERALIZABILITY FROM CLINICAL TRIALS)

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Before randomization

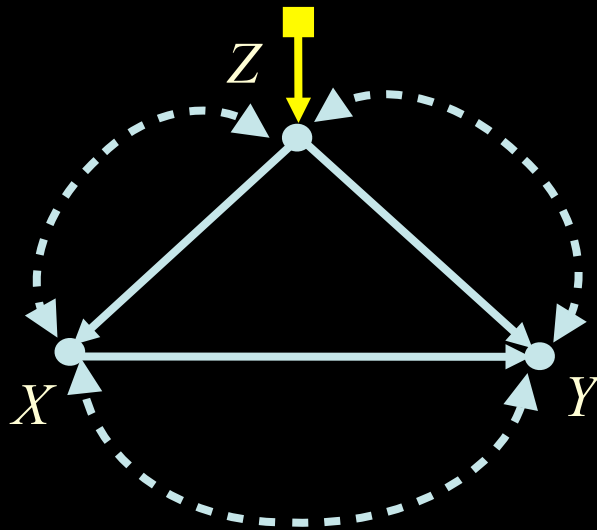


After randomization

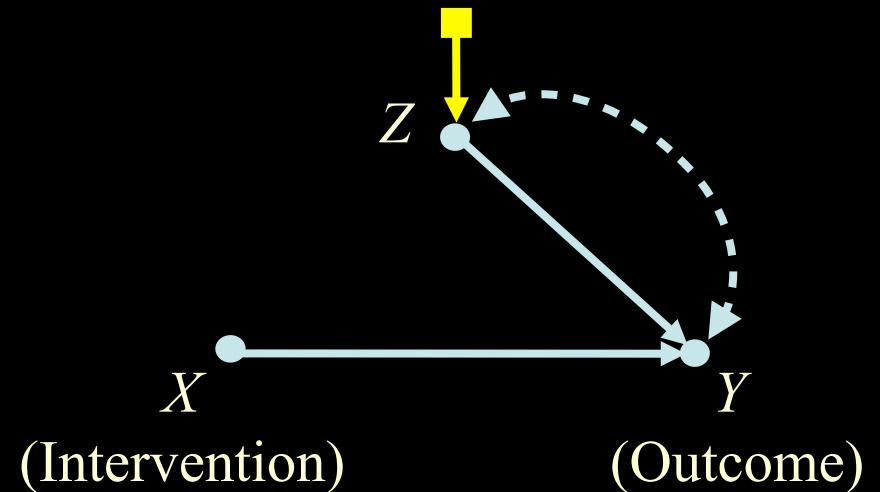


# IS THE GOLD STANDARD GOLDEN? (GENERALIZABILITY FROM CLINICAL TRIALS)

Before randomization



After randomization



**Lesson.** Even if we have a perfect RCT, one still needs to go through a Transportability exercise. TR theory is unavoidable.

# CausalAI LAB

## Big Picture



# CausalAI Lab - Big Picture



# CausalAI Lab - Big Picture

**Postdoc  
Available**

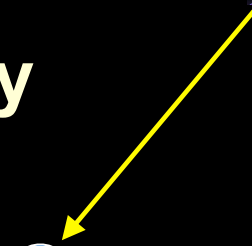
# CausalAI Lab - Big Picture

**Postdoc  
Available**

## **Structural Causal Models**



## Structural Causal Models



### 1. Explainability

(Effect identification and decomposition, Bias Analysis and Fairness, Robustness and Generalizability)

## Structural Causal Models

### 1. Explainability

(Effect identification and decomposition, Bias Analysis and Fairness, Robustness and Generalizability)



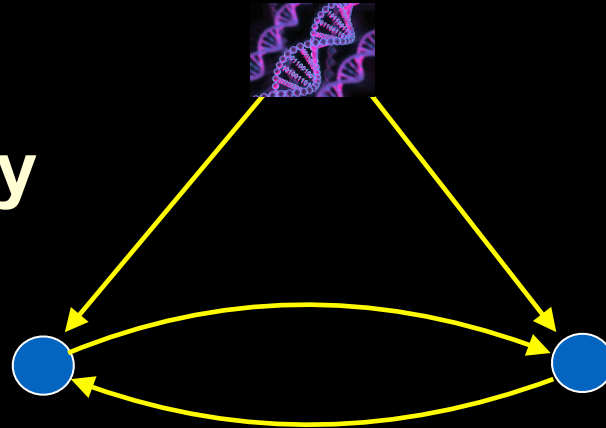
### 2. Decision-Making

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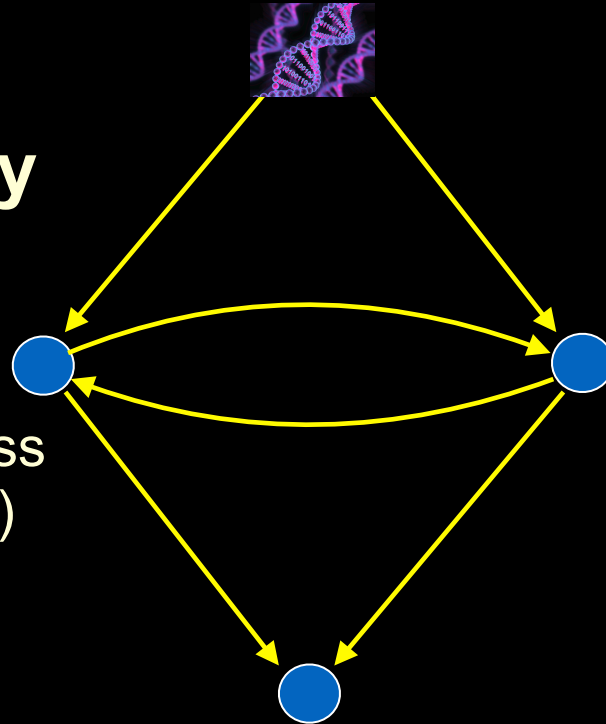
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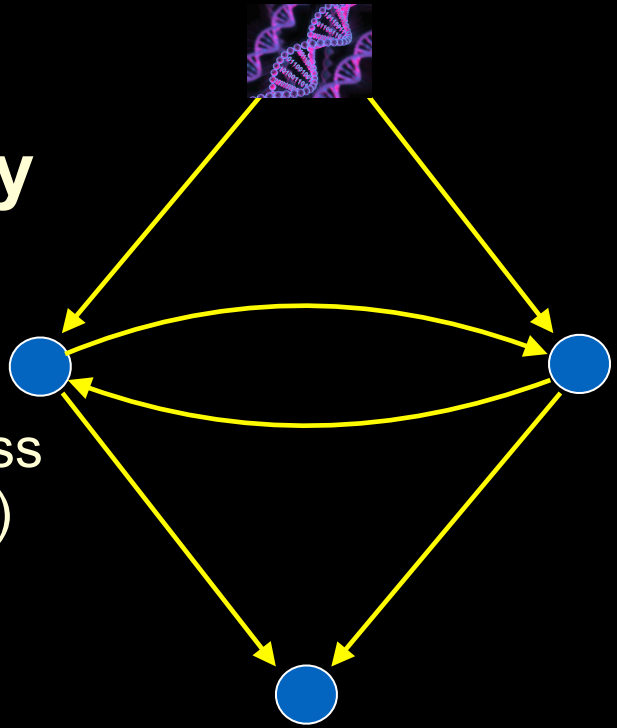
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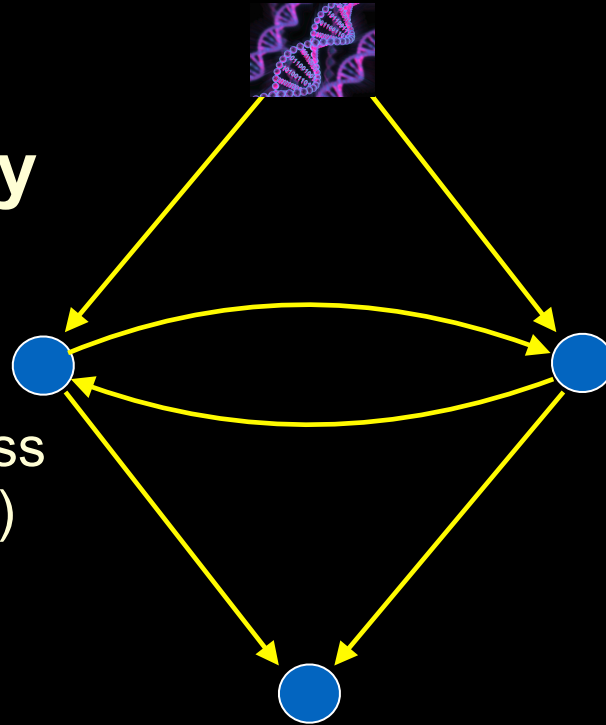
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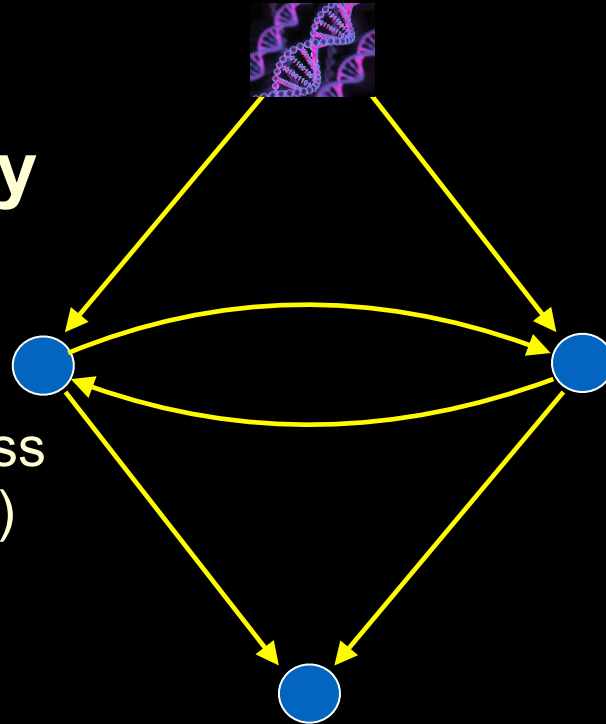
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# CONCLUSIONS

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  - Strategy: combine causal inference theory with AI-ML techniques to automate the process and close the scientific discovery loop.

“Development of Western Science is based on two great achievements, the invention of the **formal logical system** (in Euclidean geometry) by the Greek philosophers, and the discovery of the possibility to find out causal relationships by **systematic experiment** (during the Renaissance)”.  
Albert Einstein.

“Imagine how much harder physics would be if electrons had feelings!”. Richard Feynman.

**THANK YOU!**

# CAUSAL FAIRNESS ANALYSIS

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NeurIPS'18  
AAAI'19



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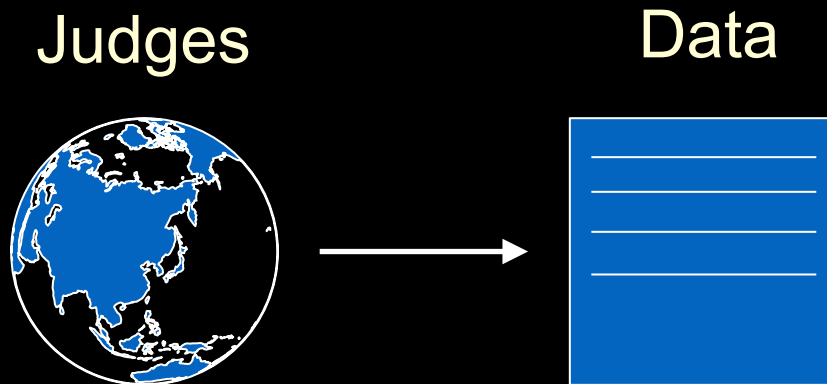
Judges



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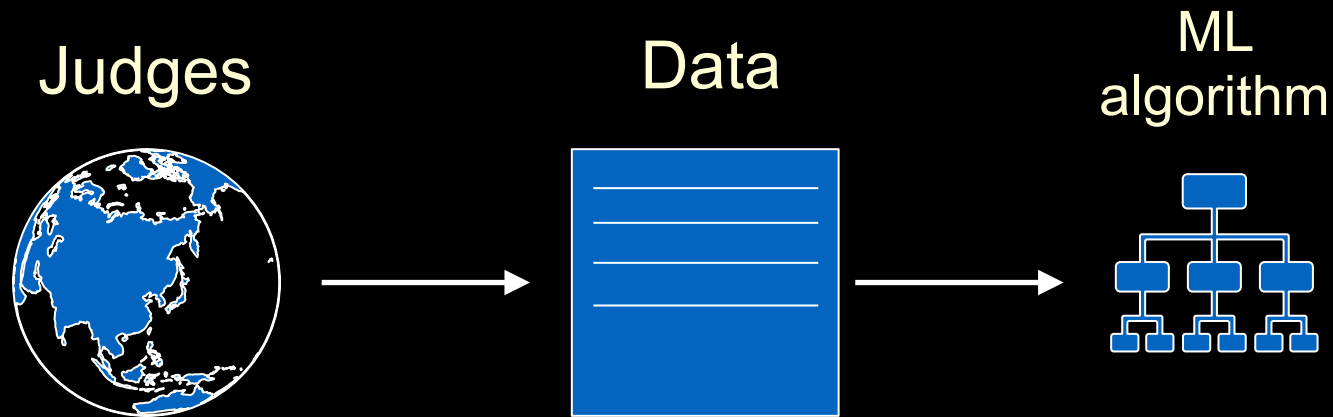
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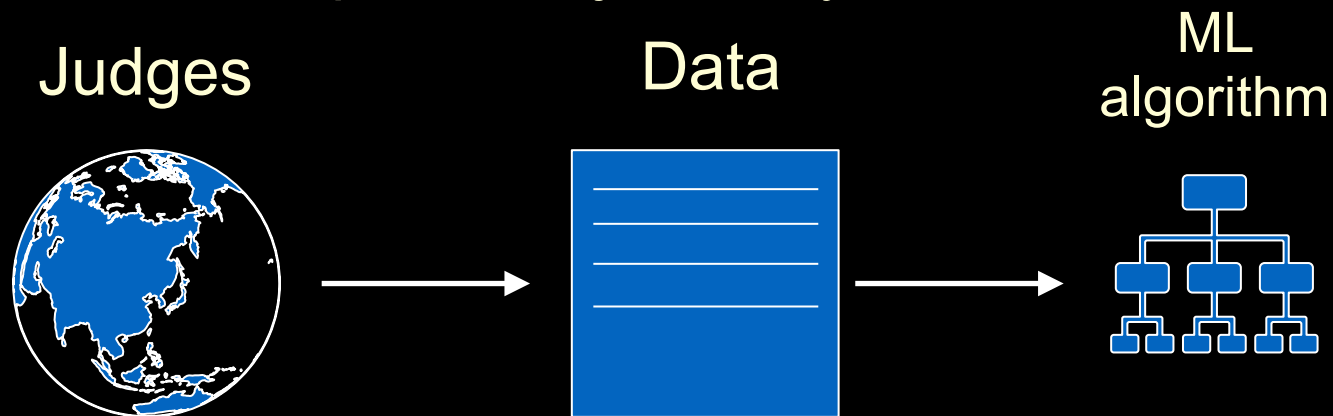
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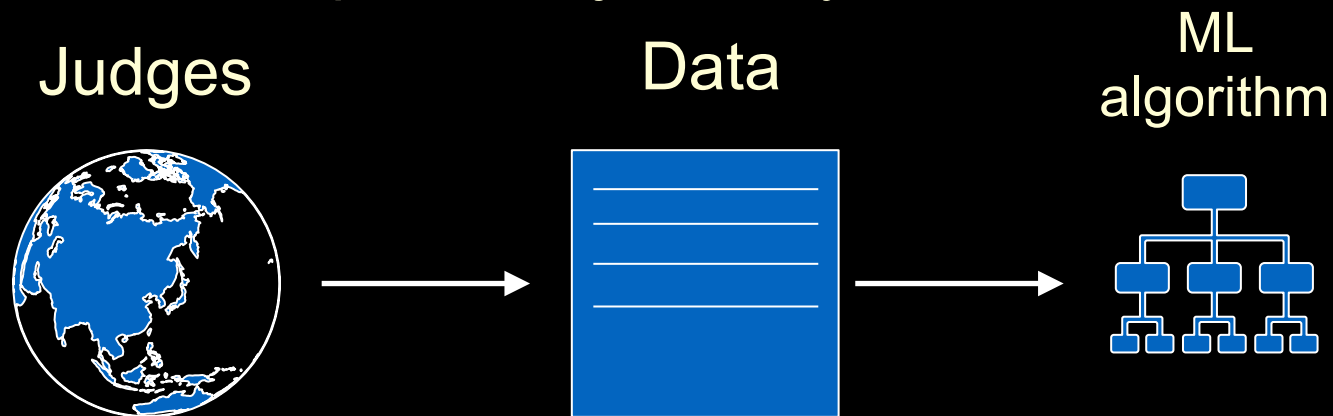


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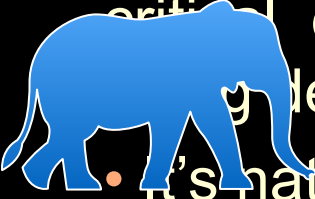


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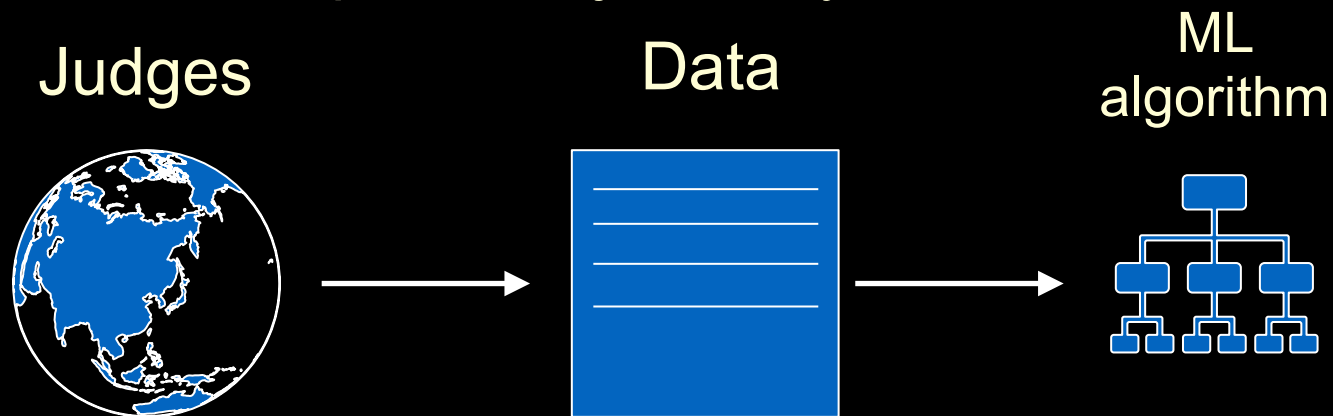
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**Question.** If the data cannot be used as baseline (or oracle), what can we, machine learners, really do?

- Consider



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NeurIPS'18  
AAAI'19

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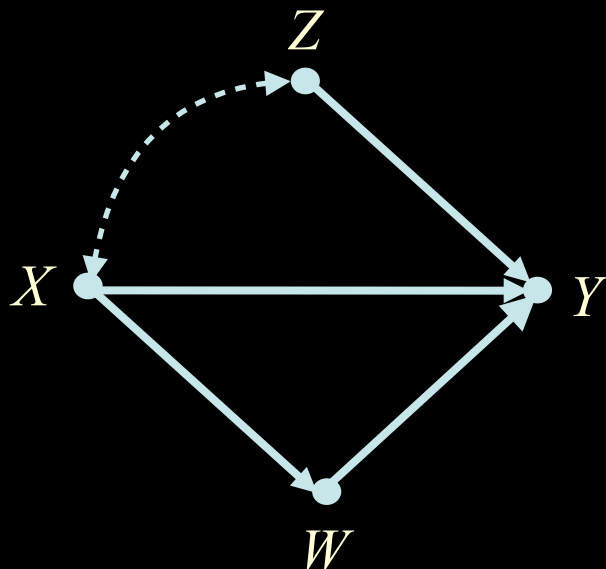
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- **Question.** How can we disentangle “the reasons” for the judges to be acting in the way they did from the observed reality and data? How to measure the underlying causal mechanisms that are unobserved?

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- Example: Assume  $X$  is the protected attribute, e.g., religious beliefs,  $Y$  is the outcome of interest, hiring decision, and  $Z$  and  $W$  are covariates encoding, respectively, the educational level and proximity to work of the applicant.

Causal Model

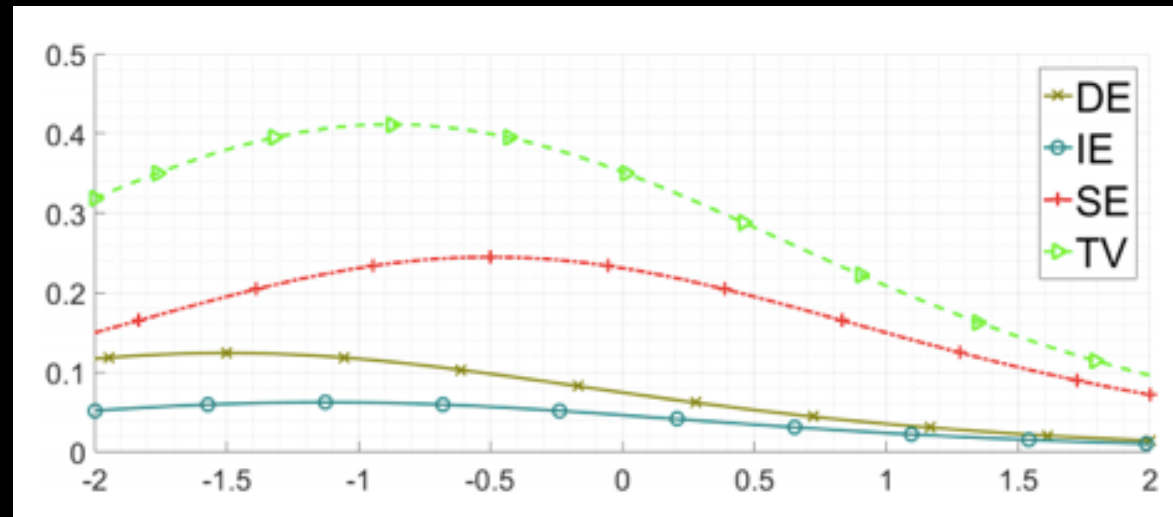
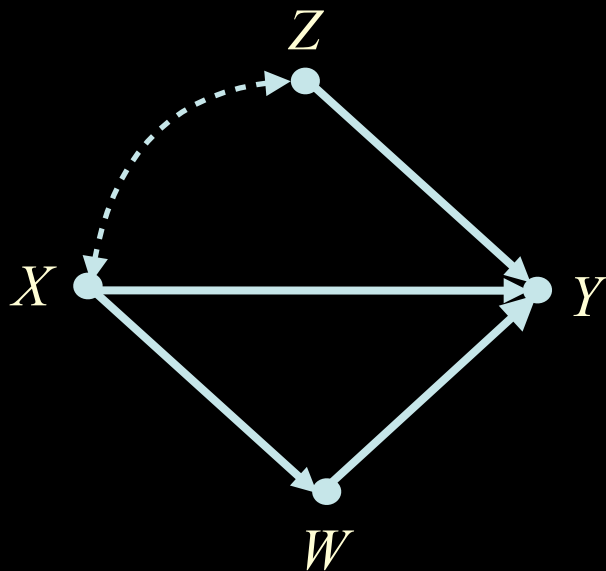




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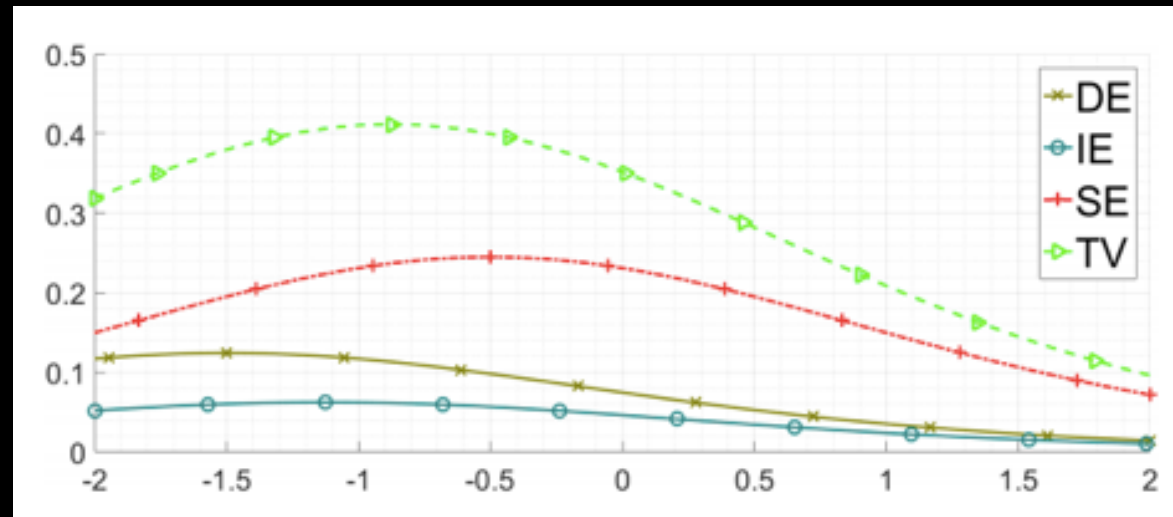
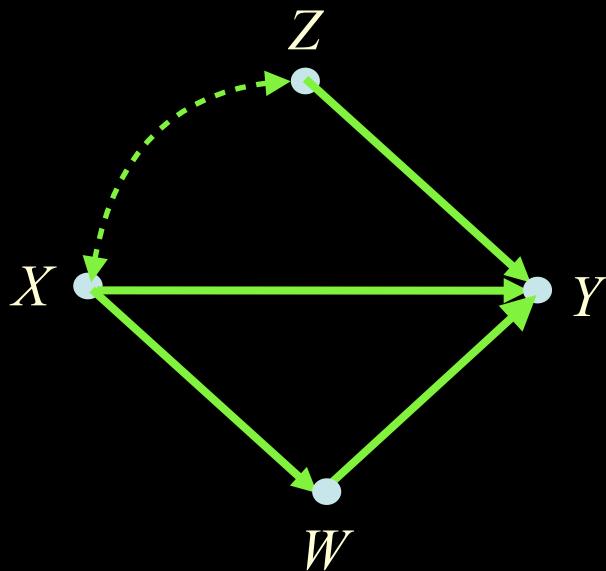
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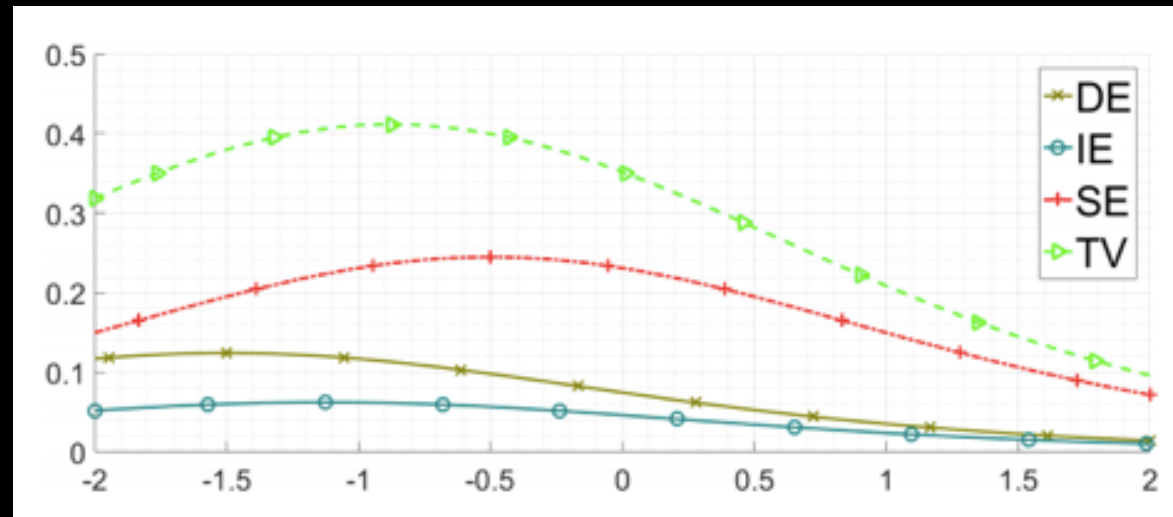
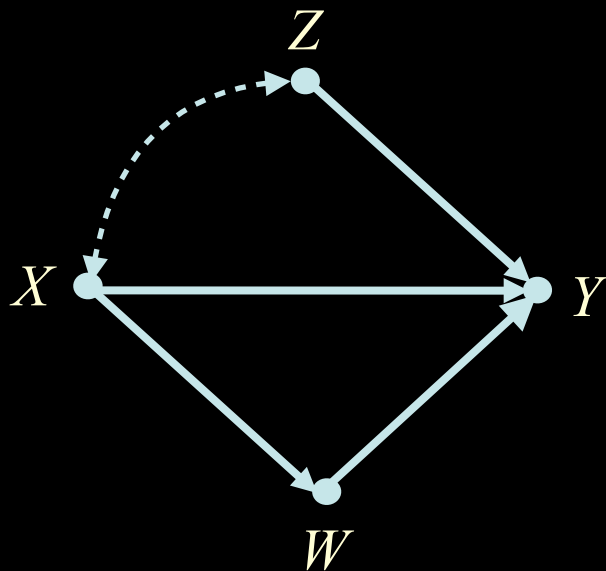
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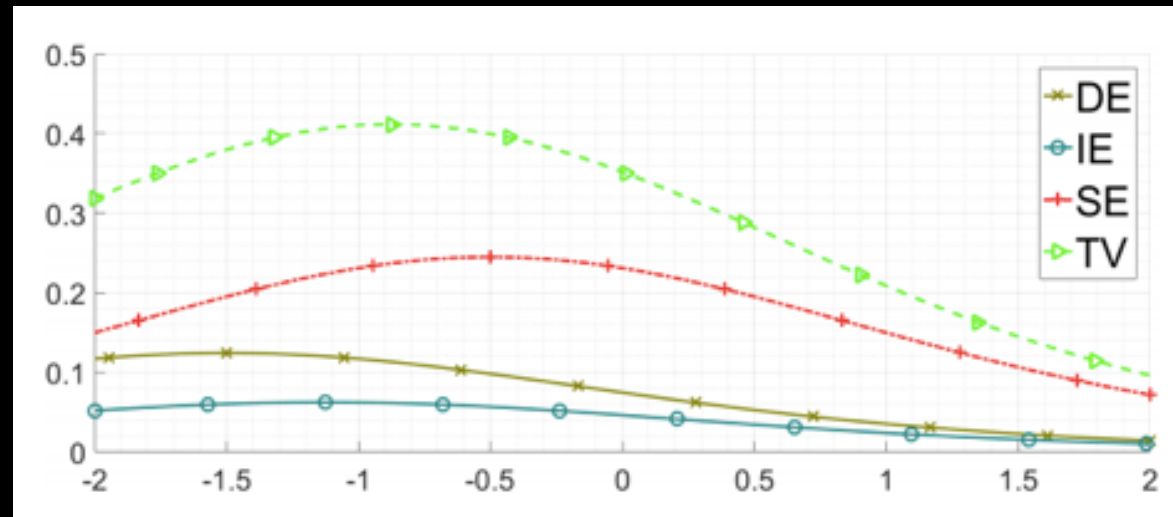
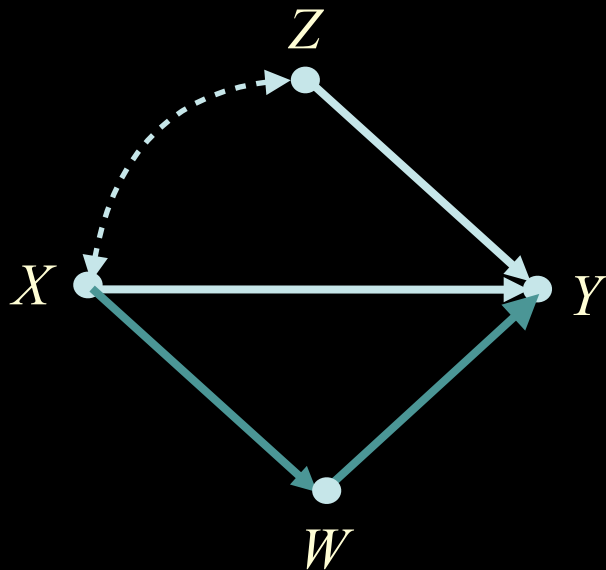
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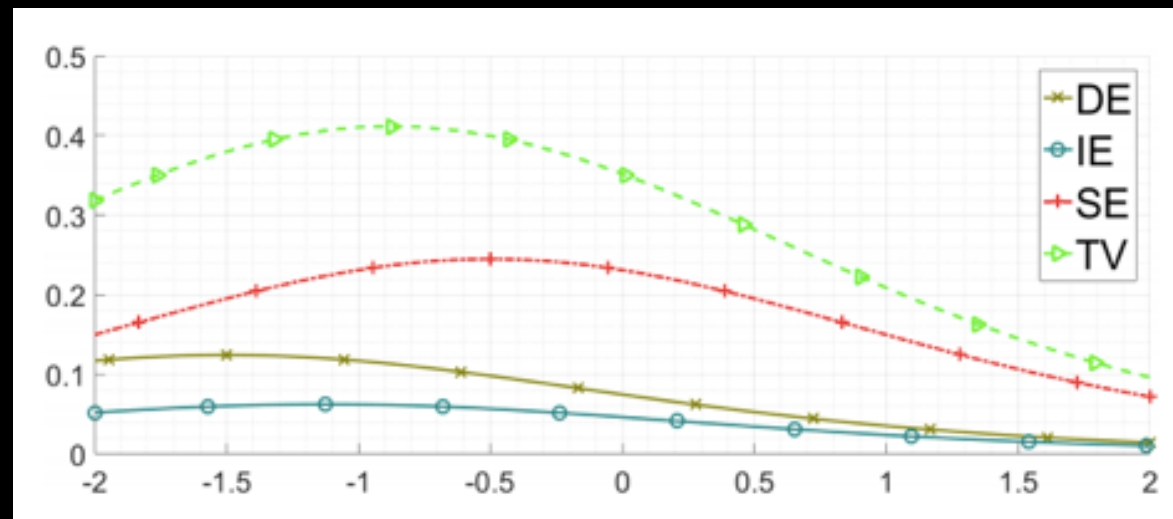
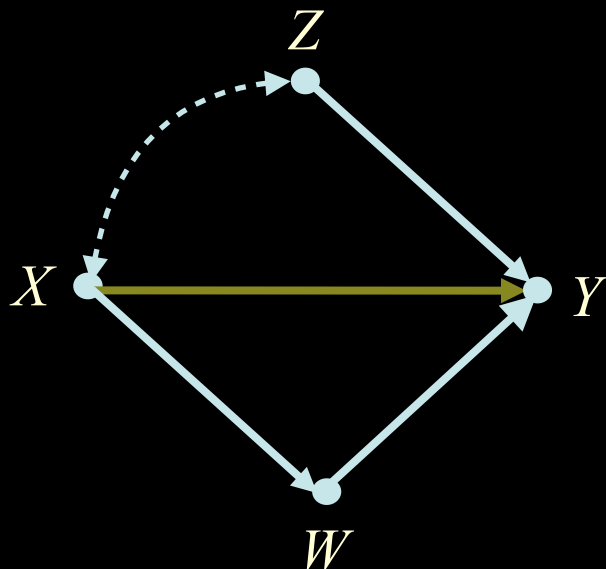
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